## **Archdiocese of Philadelphia**



Curriculum Standards

**English Language Arts and Mathematics** 

**Grade Four** 

#### INTRODUCTION

The mission statement of the Office of Catholic Education boldly proclaims that:

Catholic Schools form Catholic students to be full and practicing members of the Church, are centers of evangelization that call all to live fully the message of Jesus Christ, and are centers of academic excellence that rigorously prepare students to be life-long learners and contributing members of the global community.

From this we draw our primary focus, the faith formation of our students. Of major importance, too, is the academic preparation our students receive which will enable them to be college- and career-ready upon commencement from their experience in archdiocesan schools.

This document is a response to the call to prepare our students to become "contributing members of the global community." It is the product of an in-depth study of the data related to existing curriculum, current research, input from respected professional organizations and hours of intense work and dialogue on the part of teachers and administrators from throughout the archdiocese.

Our data study encouraged us to build on the patterns of excellence which have been a hallmark of education in Archdiocesan schools. A review of the existing curriculum and input from many teachers called us to re-focus curriculum content so that instruction and learning would incorporate higher-level thinking and in-depth teaching. At the recommendation of the National Governors' Association, we are moving forward with the adoption of the Common Core State Standards as the basis for curriculum content.

Included in this document are the Common Core State Standards for this level as well as the implementation guides prepared by the curriculum committee members who spent a great deal of time working on them.

As we move forward in the period of transition to full adoption of the Standards and to assessing archdiocesan students using national assessments, we feel confident that our teachers will continue to move forward with the same dedication that will prepare our students to stand shoulder-to-shoulder with the best students both nationally and internationally.

#### **ACKNOWLEDGEMENTS**

We would like to acknowledge the following curriculum committee members for their tireless efforts in the preparation of this document:

| English Language Arts            | Mathematics                |                  |
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We are also grateful to the **Elementary Technology Committee** for preparing web links to these guidelines.

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#### NOTE:

The English Language Arts and Mathematics content are intentionally contained in the same document. With research indicating that skills should be presented in an integrated context, it is the hope that teachers will be more aware of the total curriculum at this level rather than isolated subject matter and make deliberate connections between skills presented in each area.

Also included at each level (with the exception of Kindergarten) are the Common Core State Standards for the grade below and the grade above each level. These are placed here so that, during the transition period leading up to full implementation of the Standards, the teacher is aware of skills that should have been presented at an earlier level and makes plans to incorporate these skills in the event that they have not been presented. It is important, too, that skills designated for higher levels are not anticipated at the current instructional level.



# English Language Arts

## **Grade 4**

Common Core State Standards – English Language Arts – Grade 3

Common Core State Standards – English Language Arts – Grade 4

Common Core Standards – English Language Arts – Grade 5

Archdiocesan Implementation Guides – Grade 4

## **Key Points In English Language Arts**

#### Reading

- The standards establish a "staircase" of increasing complexity in what students must be able to read so that all students are ready for the demands of college- and career-level reading no later than the end of high school. The standards also require the progressive development of reading comprehension so that students advancing through the grades are able to gain more from whatever they read.
- Through reading a diverse array of classic and contemporary literature as well as challenging informational texts in a range of subjects, students are expected to build knowledge, gain insights, explore possibilities, and broaden their perspective. Because the standards are building blocks for successful classrooms, but recognize that teachers, school districts and states need to decide on appropriate curriculum, they intentionally do not offer a reading list. Instead, they offer numerous sample texts to help teachers prepare for the school year and allow parents and students to know what to expect at the beginning of the year.
- The standards mandate certain critical types of content for all students, including classic myths and stories from around the world, foundational U.S. documents, seminal works of American literature, and the writings of Shakespeare. The standards appropriately defer the many remaining decisions about what and how to teach to states, districts, and schools.

#### Writing

- The ability to write logical arguments based on substantive claims, sound reasoning, and relevant evidence is a cornerstone of the writing standards, with opinion writing---a basic form of argument---extending down into the earliest grades.
- Research---both short, focused projects (such as those commonly required in the workplace) and longer term in depth
  research---"is emphasized throughout the standards but most prominently in the writing strand since a written analysis and
  presentation of findings is so often critical.
- Annotated samples of student writing accompany the standards and help establish adequate performance levels in writing arguments, informational/explanatory texts, and narratives in the various grades.

#### Speaking and Listening

• The standards require that students gain, evaluate, and present increasingly complex information, ideas, and evidence through listening and speaking as well as through media.

• An important focus of the speaking and listening standards is academic discussion in one-on-one, small-group, and whole-class settings. Formal presentations are one important way such talk occurs, but so is the more informal discussion that takes place as students collaborate to answer questions, build understanding, and solve problems.

#### Language

- The standards expect that students will grow their vocabularies through a mix of conversations, direct instruction, and reading. The standards will help students determine word meanings, appreciate the nuances of words, and steadily expand their repertoire of words and phrases.
- The standards help prepare students for real life experience at college and in 21st century careers. The standards recognize that students must be able to use formal English in their writing and speaking but that they must also be able to make informed, skillful choices among the many ways to express themselves through language.
- Vocabulary and conventions are treated in their own strand not because skills in these areas should be handled in isolation but because their use extends across reading, writing, speaking, and listening.

#### Media and Technology

• Just as media and technology are integrated in school and life in the twenty-first century, skills related to media use (both critical analysis and production of media) are integrated throughout the standards.



## **Key Features of the Standards**

**Reading:** Text complexity and the growth of comprehension

The Reading standards place equal emphasis on the sophistication of what students read and the skill with which they read. Standard 10 defines a grade-by-grade "staircase" of increasing text complexity that rises from beginning reading to the college and career readiness level. Whatever they are reading, students must also show a steadily growing ability to discern more from and make fuller use of text, including making an increasing number of connections among ideas and between texts, considering a wider range of textual evidence, and becoming more sensitive to inconsistencies, ambiguities, and poor reasoning in texts.

Writing: Text types, responding to reading, and research

The Standards acknowledge the fact that whereas some writing skills, such as the ability to plan, revise, edit, and publish, are applicable to many types writing, other skills are more properly defined in terms of specific writing types: arguments, informative/explanatory texts, and narratives. Standard 9 stresses the importance of the writing-reading connection by requiring students to draw upon and write about evidence from literary and informational texts. Because of the centrality of writing to most forms of inquiry, research standards are prominently included in this strand, though skills important to research are infused throughout the document.

#### Speaking and Listening: Flexible communication and collaboration

Including but not limited to skills necessary for formal presentations, the Speaking and Listening standards require students to develop a range of broadly useful oral communication and interpersonal skills. Students must learn to work together, express and listen carefully to ideas, integrate information from oral, visual, quantitative, and media sources, evaluate what they hear, use media and visual displays strategically to help achieve communicative purposes, and adapt speech to context and task.

Language: Conventions, effective use, and vocabulary

The Language standards include the essential "rules" of standard written and spoken English, but they also approach language as a matter of craft and informed choice among alternatives. The vocabulary standards focus on understanding words and phrases, their relationships, and their nuances and on acquiring new vocabulary, particularly general academic and domain-specific words and phrases.

#### Appendices A, B, and C

- Appendix A contains supplementary material on reading, writing, speaking and listening, and language as well as a glossary of key terms.
- Appendix B consists of text exemplars illustrating the complexity, quality, and range of reading appropriate for various grade levels with accompanying sample performance tasks.
- Appendix C includes annotated samples demonstrating at least adequate performance in student writing at various grade levels

## **Anchor Standards for Reading**

The K–5 standards on the following pages define what students should understand and be able to do by the end of each grade. They correspond to the College and Career Readiness (CCR) anchor standards below by number. The CCR and grade-specific standards are necessary complements—the former providing broad standards, the latter providing additional specificity—that together define the skills and understandings that all students must demonstrate.

#### **Key Ideas and Details**

- 1. Read closely to determine what the text says explicitly and to make logical inferences from it; cite specific textual evidence when writing or speaking to support conclusions drawn from the text.
- 2. Determine central ideas or themes of a text and analyze their development; summarize the key supporting details and ideas.
- 3. Analyze how and why individuals, events, and ideas develop and interact over the course of a text.

#### **Craft and Structure**

- 4. Interpret words and phrases as they are used in a text, including determining technical, connotative, and figurative meanings, and analyze how specific word choices shape meaning or tone.
- 5. Analyze the structure of texts, including how specific sentences, paragraphs, and larger portions of the text (e.g., a section, chapter, scene, or stanza) relate to each other and the whole.
- 6. Assess how point of view or purpose shapes the content and style of a text.

#### Integration of Knowledge and Ideas

7. Integrate and evaluate content presented in diverse media and formats, including visually and quantitatively, as well as in words.<sup>1</sup>

- 8. Delineate and evaluate the argument and specific claims in a text, including the validity of the reasoning as well as the relevance and sufficiency of the evidence.
- 9. Analyze how two or more texts address similar themes or topics in order to build knowledge or to compare the approaches the authors take.

#### Range of Reading and Level of Text Complexity

10. Read and comprehend complex literary and informational texts independently and proficiently.

## **Anchor Standards for Writing**

The K–5 standards on the following pages define what students should understand and be able to do by the end of each grade. They correspond to the College and Career Readiness (CCR) anchor standards below by number. The CCR and grade-specific standards are necessary complements—the former providing broad standards, the latter providing additional specificity—that together define the skills and understandings that all students must demonstrate.

#### **Text Types and Purposes**

- 1. Write arguments to support claims in an analysis of substantive topics or texts, using valid reasoning and relevant and sufficient evidence.
- 2. Write informative/explanatory texts to examine and convey complex ideas and information clearly and accurately through the effective selection, organization, and analysis of content.
- 3. Write narratives to develop real or imagined experiences or events using effective technique, well-chosen details, and well-structured event sequences.

#### **Production and Distribution of Writing**

- 4. Produce clear and coherent writing in which the development, organization, and style are appropriate to task, purpose, and audience.
- 5. Develop and strengthen writing as needed by planning, revising, editing, rewriting, or trying a new approach.
- 6. Use technology, including the Internet, to produce and publish writing and to interact and collaborate with others.

#### Research to Build and Present Knowledge

- 7. Conduct short as well as more sustained research projects based on focused questions, demonstrating understanding of the subject under investigation.
- 8. Gather relevant information from multiple print and digital sources, assess the credibility and accuracy of each source, and integrate the information while avoiding plagiarism.
- 9. Draw evidence from literary or informational texts to support analysis, reflection, and research.

#### Range of Writing

10. Write routinely over extended time frames (time for research, reflection, and revision) and shorter time frames (a single sitting or a day or two) for a range of tasks, purposes, and audiences.

#### Note on range and content in student writing

To build a foundation for college and career readiness, students need to learn to use writing as a way of offering and supporting opinions, demonstrating understanding of the subjects they are studying, and conveying real and imagined experiences and events. They learn to appreciate that a key purpose of writing is to communicate clearly to an external, sometimes unfamiliar audience, and they begin to adapt the form and content of their writing to accomplish a particular task and purpose. They develop the capacity to build knowledge on a subject through research projects and to respond analytically to literary and informational sources. To meet these goals, students must devote significant time and effort to writing, producing numerous pieces over short and extended time frames throughout the year.

## **Anchor Standards for Speaking and Listening**

#### **Comprehension and Collaboration**

- 1. Prepare for and participate effectively in a range of conversations and collaborations with diverse partners, building on others' ideas and expressing their own clearly and persuasively.
- 2. Integrate and evaluate information presented in diverse media and formats, including visually, quantitatively, and orally.
- 3. Evaluate a speaker's point of view, reasoning, and use of evidence and rhetoric.

#### Presentation of Knowledge and Ideas

- 4. Present information, findings, and supporting evidence such that listeners can follow the line of reasoning and the organization, development, and style are appropriate to task, purpose, and audience.
- 5. Make strategic use of digital media and visual displays of data to express information and enhance understanding of presentations.
- 6. Adapt speech to a variety of contexts and communicative tasks, demonstrating command of formal English when indicated or appropriate.

#### Note on range and content of student speaking and listening

To build a foundation for college and career readiness, students must have ample opportunities to take part in a variety of rich, structured conversations—as part of a whole class, in small groups, and with a partner. Being productive members of these conversations requires that students contribute accurate, relevant information; respond to and develop what others have said; make comparisons and contrasts; and analyze and synthesize a multitude of ideas in various domains.

New technologies have broadened and expanded the role that speaking and listening play in acquiring and sharing knowledge and have tightened their link to other forms of communication. Digital texts confront students with the potential for continually updated content and dynamically changing combinations of words, graphics, images, hyperlinks, and embedded video and audio.

## **Anchor Standards for Language**

The K–5 standards on the following pages define what students should understand and be able to do by the end of each grade. They correspond to the College and Career Readiness (CCR) anchor standards below by number. The CCR and grade-specific standards are necessary complements—the former providing broad standards, the latter providing additional specificity—that together define the skills and understandings that all students must demonstrate.

#### **Conventions of Standard English**

- 1. Demonstrate command of the conventions of standard English grammar and usage when writing or speaking.
- 2. Demonstrate command of the conventions of standard English capitalization, punctuation, and spelling when writing.

#### **Knowledge of Language**

3. Apply knowledge of language to understand how language functions in different contexts, to make effective choices for meaning or style, and to comprehend more fully when reading or listening.

#### **Vocabulary Acquisition and Use**

- 4. Determine or clarify the meaning of unknown and multiple-meaning words and phrases by using context clues, analyzing meaningful word parts, and consulting general and specialized reference materials, as appropriate.
- 5. Demonstrate understanding of word relationships and nuances in word meanings.
- 6. Acquire and use accurately a range of general academic and domain-specific words and phrases sufficient for reading, writing, speaking, and listening at the college and career readiness level; demonstrate independence in gathering vocabulary knowledge when encountering an unknown term important to comprehension or expression.

#### Note on range and content of student language use

To build a foundation for college and career readiness in language, students must gain control over many conventions of standard English grammar, usage, and mechanics as well as learn other ways to use language to convey meaning effectively. They must also be able to determine or clarify the meaning of grade-appropriate words encountered through listening, reading, and media use; come to appreciate that words have nonliteral meanings, shadings of meaning, and relationships to other words; and expand their vocabulary in the course of studying content. The inclusion of Language standards in their own strand should not be taken as an indication that skills related to conventions, effective language use, and vocabulary are unimportant to reading, writing, speaking, and listening; indeed, they are inseparable from such contexts.

#### **ELA Standards for Grade 3**

## **Reading Standards for Literature**

#### **Key Ideas and Details**

- RL.3.1 Ask and answer questions to demonstrate understanding of a text, referring explicitly to the text as the basis for the answers.
- RL.3..2. Recount stories, including fables, folktales, and myths from diverse cultures; determine the central message, lesson, or moral and explain how it is conveyed through key details in the text.
- RL.3..3. Describe characters in a story (e.g., their traits, motivations, or feelings) and explain how their actions contribute to the sequence of events.

#### **B. Craft and Structure**

- RL.3..4. Determine the meaning of words and phrases as they are used in a text, distinguishing literal from non-literal language.
- RL.3.5. Refer to parts of stories, dramas, and poems when writing or speaking about a text, using terms such as chapter, scene, and stanza; describe how each successive part builds on earlier sections.
- RL.3..6. Distinguish their own point of view from that of the narrator or those of the characters.

#### Integration of Knowledge and Ideas

- RL.3.7. Explain how specific aspects of a text's illustrations contribute to what is conveyed by the words in a story (e.g., create mood, emphasize aspects of a character or setting).
- RL.3.9. Compare and contrast the themes, settings, and plots of stories written by the same author about the same or similar characters (e.g., in books from a series).

#### Range of Reading and Level of Text Complexity

RL.3..RL.10. By the end of the year, read and comprehend literature, including stories, dramas, and poetry, at the high end of the grades 2–3 text complexity band independently and proficiently.

## **Reading Standards for Informational Text**

#### **Key Ideas and Details**

- RI.3.1. Ask and answer questions to demonstrate understanding of a text, referring explicitly to the text as the basis for the answers.
- RI.3.2. Determine the main idea of a text; recount the key details and explain how they support the main idea.
- RI.3. Describe the relationship between a series of historical events, scientific ideas or concepts, or steps in technical procedures in a text, using language that pertains to time, sequence, and cause/effect.

#### **Craft and Structure**

- RI.3.4. Determine the meaning of general academic and domain-specific words and phrases in a text relevant to a *grade 3 topic or subject* area.
- RI.3.5. Use text features and search tools (e.g., key words, sidebars, hyperlinks) to locate information relevant to a given topic efficiently.
- RI.3.6. Distinguish their own point of view from that of the author of a text.

#### Integration of Knowledge and Ideas

- RI.3.7. Use information gained from illustrations (e.g., maps, photographs) and the words in a text to demonstrate understanding of the text (e.g., where, when, why, and how key events occur).
- RI.3.8. Describe the logical connection between particular sentences and paragraphs in a text (e.g., comparison, cause/effect, first/second/third in a sequence).
- RI.3.9. Compare and contrast the most important points and key details presented in two texts on the same topic.

#### Range of Reading and Level of Text Complexity

RI.3.10. By the end of the year, read and comprehend informational texts, including history/social studies, science, and technical texts, at the high end of the grades 2–3 text complexity band independently and proficiently.

## **Reading Standards: Foundational Skills**

#### **Phonics and Word Recognition**

- RF.3.3 Know and apply grade-level phonics and word analysis skills in decoding words.
  - Identify and know the meaning of the most common prefixes and derivational suffixes.
  - Decode words with common Latin suffixes.
  - Decode multi-syllable words.
  - Read grade-appropriate irregularly spelled words.

#### **Fluency**

- RF.3.4. Read with sufficient accuracy and fluency to support comprehension.
  - Read on-level text with purpose and understanding.
  - Read on-level prose and poetry orally with accuracy, appropriate rate, and expression on successive readings
  - Use context to confirm or self-correct word recognition and understanding, rereading as necessary.

## **Writing Standards**

#### **Text Types and Purposes**

- W.3.1 Write opinion pieces on topics or texts, supporting a point of view with reasons.
  - Introduce the topic or text they are writing about, state an opinion, and create an organizational structure that lists reasons.
  - Provide reasons that support the opinion.
  - Use linking words and phrases (e.g., because, therefore, since, for example) to connect opinion and reasons.
  - Provide a concluding statement or section.

- W.3.2. Write informative/explanatory texts to examine a topic and convey ideas and information clearly.
  - Introduce a topic and group related information together; include illustrations when useful to aiding comprehension.
  - Develop the topic with facts, definitions, and details.
  - Use linking words and phrases (e.g., also, another, and, more, but) to connect ideas within categories of information.
  - Provide a concluding statement or section.
- W.3.3. Write narratives to develop real or imagined experiences or events using effective technique, descriptive details, and clear event sequences.
  - Establish a situation and introduce a narrator and/or characters; organize an event sequence that unfolds naturally.
  - Use dialogue and descriptions of actions, thoughts, and feelings to develop experiences and events or show the response of characters to situations.
  - Use temporal words and phrases to signal event order.
  - Provide a sense of closure.

#### **Production and Distribution of Writing**

- W.3.4. With guidance and support from adults, produce writing in which the development and organization are appropriate to task and purpose.
- W.3.5. With guidance and support from peers and adults, develop and strengthen writing as needed by planning, revising, and editing.
- W.3.6. With guidance and support from adults, use technology to produce and publish writing (using keyboarding skills) as well as to interact and collaborate with others.

#### Research to Build and Present Knowledge

- W.3.7 Conduct short research projects that build knowledge about a topic.
- W.3.8. Recall information from experiences or gather information from print and digital sources; take brief notes on sources and sort evidence into provided categories.

#### Range of Writing

W.3.10. Write routinely over extended time frames (time for research, reflection, and revision) and shorter time frames (a single sitting or a day or two) for a range of discipline-specific tasks, purposes, and audiences.

## **Speaking and Listening Standards**

#### **Comprehension and Collaboration**

- SL.3.1. Engage effectively in a range of collaborative discussions (one-on-one, in groups, and teacher-led) with diverse partners on *grade 3 topics and texts*, building on others' ideas and expressing their own clearly.
  - Come to discussions prepared, having read or studied required material; explicitly draw on that preparation and other information known about the topic to explore ideas under discussion.
  - Follow agreed-upon rules for discussions (e.g., gaining the floor in respectful ways, listening to others with care, speaking one at a time about the topics and texts under discussion).
  - Ask questions to check understanding of information presented, stay on topic, and link their comments to the remarks of others.
  - Explain their own ideas and understanding in light of the discussion.
- SL.3.2. Determine the main ideas and supporting details of a text read aloud or information presented in diverse media and formats, including visually, quantitatively, and orally.
- SL.3.3. Ask and answer questions about information from a speaker, offering appropriate elaboration and detail.

#### Presentation of Knowledge and Ideas

- SL.3.4. Report on a topic or text, tell a story, or recount an experience with appropriate facts and relevant, descriptive details, speaking clearly at an understandable pace.
- SL.3.5. Create engaging audio recordings of stories or poems that demonstrate fluid reading at an understandable pace; add visual displays when appropriate to emphasize or enhance certain facts or details.
- SL.3.6. Speak in complete sentences when appropriate to task and situation in order to provide requested detail or clarification.

## **Language Standards**

#### **Conventions of Standard English**

- L.3.1. Demonstrate command of the conventions of standard English grammar and usage when writing or speaking.
  - Explain the function of nouns, pronouns, verbs, adjectives, and adverbs in general and their functions in particular sentences.
  - Form and use regular and irregular plural nouns.
  - Use abstract nouns (e.g., childhood).
  - Form and use regular and irregular verbs.
  - Form and use the simple (e.g., I walked; I walk; I will walk) verb tenses.
  - Ensure subject-verb and pronoun-antecedent agreement.
  - Form and use comparative and superlative adjectives and adverbs, and choose between them depending on what is to be modified.
  - Use coordinating and subordinating conjunctions.
  - Produce simple, compound, and complex sentences.
- L.3.2. Demonstrate command of the conventions of standard English capitalization, punctuation, and spelling when writing.
  - Capitalize appropriate words in titles.
  - Use commas in addresses.
  - Use commas and quotation marks in dialogue.
  - Form and use possessives.
  - Use conventional spelling for high-frequency and other studied words and for adding suffixes to base words (e.g., sitting, smiled, cries, happiness).
  - Use spelling patterns and generalizations (e.g., word families, position-based spellings, syllable patterns, ending rules, meaningful word parts) in writing words.
  - Consult reference materials, including beginning dictionaries, as needed to check and correct spellings.

#### **Knowledge of Language**

- L.3.3. Use knowledge of language and its conventions when writing, speaking, reading, or listening.
  - Choose words and phrases for effect.
  - Recognize and observe differences between the conventions of spoken and written standard English.

#### **Vocabulary Acquisition and Use**

- L.3.4. Determine or clarify the meaning of unknown and multiple-meaning word and phrases based on *grade 3 reading and content,* choosing flexibly from a range of strategies.
  - Use sentence-level context as a clue to the meaning of a word or phrase.
  - Determine the meaning of the new word formed when a known affix is added to a known word (e.g., agreeable/disagreeable, comfortable/uncomfortable, care/careless, heat/preheat).
  - Use a known root word as a clue to the meaning of an unknown word with the same root (e.g., company, companion).
  - Use glossaries or beginning dictionaries, both print and digital, to determine or clarify the precise meaning of key words and phrases.
  - L.3.5. Demonstrate understanding of word relationships and nuances in word meanings.
    - Distinguish the literal and non-literal meanings of words and phrases in context (e.g., take steps).
    - Identify real-life connections between words and their use (e.g., describe people who are friendly or helpful).
    - Distinguish shades of meaning among related words that describe states of mind or degrees of certainty (e.g., knew, believed, suspected, heard, wondered).
  - L.3.6. Acquire and use accurately grade-appropriate conversational, general academic, and domain-specific words and phrases, including those that signal spatial and temporal relationships (e.g., *After dinner that night we went looking for them*).

#### **ELA Standards – Grade 4**

### **Reading Standards for Literature**

#### **Key Ideas and Details**

- RL.4. 1. Refer to details and examples in a text when explaining what the text says explicitly and when drawing inferences from the text.
- RL.4. 2. Determine a theme of a story, drama, or poem from details in the text; summarize the text.
- RL.4. 3. Describe in depth a character, setting, or event in a story or drama, drawing on specific details in the text (e.g., a character's thoughts, words, or actions).

#### **Craft and Structure**

- RL.4. 4. Determine the meaning of words and phrases as they are used in a text, including those that allude to significant characters found in mythology (e.g., Herculean).
- RL.4. 5. Explain major differences between poems, drama, and prose, and refer to the structural elements of poems (e.g., verse, rhythm, meter) and drama (e.g., casts of characters, settings, descriptions, dialogue, stage directions) when writing or speaking about a text.
- RL.4. 6. Compare and contrast the point of view from which different stories are narrated, including the difference between first- and third-person narrations.

#### Integration of Knowledge and Ideas

- RL.4. 7. Make connections between the text of a story or drama and a visual or oral presentation of the text, identifying where each version reflects specific descriptions and directions in the text.
- RL.4. 9. Compare and contrast the treatment of similar themes and topics (e.g., opposition of good and evil) and patterns of events (e.g., the quest) in stories, myths, and traditional literature from different cultures.

#### Range of Reading and Level of Text Complexity

RL.4. 10. By the end of the year, read and comprehend literature, including stories, dramas, and poetry, in the grades 4–5 text complexity band proficiently, with scaffolding as needed at the high end of the range.

## **Reading Standards for Informational Text**

#### **Key Ideas and Details**

- RI.4.1. Refer to details and examples in a text when explaining what the text says explicitly and when drawing inferences from the text.
- RI.4.2. Determine the main idea of a text and explain how it is supported by key details; summarize the text.
- RI.4.3. Explain events, procedures, ideas, or concepts in a historical, scientific, or technical text, including what happened and why, based on specific information in the text.

#### **Craft and Structure**

- RI.4.4. Determine the meaning of general academic and domain-specific words or phrases in a text relevant to a *grade 4 topic or subject area*.
- RI.4.5. Describe the overall structure (e.g., chronology, comparison, cause/effect, problem/solution) of events, ideas, concepts, or information in a text or part of a text.
- RI.4.6. Compare and contrast a firsthand and secondhand account of the same event or topic; describe the differences in focus and the information provided.

#### Integration of Knowledge and Ideas

- RI.4.7. Interpret information presented visually, orally, or quantitatively (e.g., in charts, graphs, diagrams, time lines, animations, or interactive elements on Web pages) and explain how the information contributes to an understanding of the text in which it appears.
- RI.4.8. Explain how an author uses reasons and evidence to support particular points in a text.
- RI.4.9. Integrate information from two texts on the same topic in order to write or speak about the subject knowledgeably.

#### Range of Reading and Level of Text Complexity

RI.4.10. By the end of year, read and comprehend informational texts, including history/social studies, science, and technical texts, in the grades 4–5 text complexity band proficiently, with scaffolding as needed at the high end of the range.

## **Reading Standards: Foundational Skills**

#### **Phonics and Phonemic Awareness**

RF4.3. Know and apply grade-level phonics and word analysis skills in decoding words.

• Use combined knowledge of all letter-sound correspondences, syllabication patterns, and morphology (e.g., roots and affixes) to read accurately unfamiliar multisyllabic words in context and out of context.

#### **Fluency**

RF4.4. Read with sufficient accuracy and fluency to support comprehension.

- Read on-level text with purpose and understanding.
- Read on-level prose and poetry orally with accuracy, appropriate rate, and expression on successive readings.
- Use context to confirm or self-correct word recognition and understanding, rereading as necessary.

## **Writing Standards**

#### **Text Types and Purposes**

- W.4.1. Write opinion pieces on topics or texts, supporting a point of view with reasons and information.
  - Introduce a topic or text clearly, state an opinion, and create an organizational structure in which related ideas are grouped to support the writer's purpose.
  - Provide reasons that are supported by facts and details.
  - Link opinion and reasons using words and phrases (e.g., for instance, in order to, in addition).
  - Provide a concluding statement or section related to the opinion presented.

#### W.4.2. Write informative/explanatory texts to examine a topic and convey ideas and information clearly.

- Introduce a topic clearly and group related information in paragraphs and sections; include formatting (e.g., headings), illustrations, and multimedia when useful to aiding comprehension.
- Develop the topic with facts, definitions, concrete details, quotations, or other information and examples related to the topic.
- Link ideas within categories of information using words and phrases (e.g., another, for example, also, because).
- Use precise language and domain-specific vocabulary to inform about or explain the topic.
- Provide a concluding statement or section related to the information or explanation presented.

## W.4.3. Write narratives to develop real or imagined experiences or events using effective technique, descriptive details, and clear event sequences.

- Orient the reader by establishing a situation and introducing a narrator and/or characters; organize an event sequence that unfolds naturally.
- Use dialogue and description to develop experiences and events or show the responses of characters to situations.
- Use a variety of transitional words and phrases to manage the sequence of events.
- Use concrete words and phrases and sensory details to convey experiences and events precisely.
- Provide a conclusion that follows from the narrated experiences or events.

#### **Production and Distribution of Writing**

- W.4.4. Produce clear and coherent writing in which the development and organization are appropriate to task, purpose, and audience.
- W.4.5. With guidance and support from peers and adults, develop and strengthen writing as needed by planning, revising, and editing.
- W.4.6. With some guidance and support from adults, use technology, including the Internet, to produce and publish writing as well as to interact and collaborate with others; demonstrate sufficient command of keyboarding skills to type a minimum of one page in a single sitting.

#### Research to Build and Present Knowledge

- W.4.7. Conduct short research projects that build knowledge through investigation of different aspects of a topic.
- W.4.8. Recall relevant information from experiences or gather relevant information from print and digital sources; take notes and categorize information, and provide a list of sources.
- W.4.9. Draw evidence from literary or informational texts to support analysis, reflection, and research.
  - Apply *grade 4 Reading standards* to literature (e.g., "Describe in depth a character, setting, or event in a story or drama, drawing on specific details in the text [e.g., a character's thoughts, words, or actions].").
  - Apply *grade 4 Reading standards* to informational texts (e.g., "Explain how an author uses reasons and evidence to support particular points in a text").

#### Range of Writing

W.4.10. Write routinely over extended time frames (time for research, reflection, and revision) and shorter time frames (a single sitting or a day or two) for a range of discipline-specific tasks, purposes, and audiences.

## **Speaking and Listening Standards**

#### **Comprehension and Collaboration**

- SL.4.1. Engage effectively in a range of collaborative discussions (one-on-one, in groups, and teacher-led) with diverse partners on *grade 4 topics and texts*, building on others' ideas and expressing their own clearly.
  - Come to discussions prepared, having read or studied required material; explicitly draw on that preparation and other information known about the topic to explore ideas under discussion.
  - Follow agreed-upon rules for discussions and carry out assigned roles.
  - Pose and respond to specific questions to clarify or follow up on information, and make comments that contribute to the
    discussion and link to the remarks of others.
  - Review the key ideas expressed and explain their own ideas and understanding in light of the discussion.
- SL.4..2. Paraphrase portions of a text read aloud or information presented in diverse media and formats, including visually, quantitatively, and orally.
- SL.4..3. Identify the reasons and evidence a speaker provides to support particular points.

#### Presentation of Knowledge and Ideas

- SL.4.4. Report on a topic or text, tell a story, or recount an experience in an organized manner, using appropriate facts and relevant, descriptive details to support main ideas or themes; speak clearly at an understandable pace.
- SL.4.5. Add audio recordings and visual displays to presentations when appropriate to enhance the development of main ideas or themes.
- SL.4.6. Differentiate between contexts that call for formal English (e.g., presenting ideas) and situations where informal discourse is appropriate (e.g., small-group discussion); use formal English when appropriate to task and situation.

## **Language Standards**

#### **Conventions of Standard English**

- L.4.1. Demonstrate command of the conventions of standard English grammar and usage when writing or speaking.
  - Use relative pronouns (who, whose, whom, which, that) and relative adverbs (where, when, why).
  - Form and use the progressive (e.g., I was walking; I am walking; I will be walking) verb tenses.
  - Use modal auxiliaries (e.g., can, may, must) to convey various conditions.
  - Order adjectives within sentences according to conventional patterns (e.g., a small red bag rather than a red small bag).
  - Form and use prepositional phrases.
  - Produce complete sentences, recognizing and correcting inappropriate fragments and run-ons.
  - Correctly use frequently confused words (e.g., to, too, two; there, their).
- L.4.2. Demonstrate command of the conventions of standard English capitalization, punctuation, and spelling when writing.
  - Use correct capitalization.
  - Use commas and quotation marks to mark direct speech and quotations from a text.
  - Use a comma before a coordinating conjunction in a compound sentence.
  - Spell grade-appropriate words correctly, consulting references as needed.

#### **Knowledge of Language**

- L.4.3. Use knowledge of language and its conventions when writing, speaking, reading, or listening.
  - Choose words and phrases to convey ideas precisely.
  - Choose punctuation for effect.
  - Differentiate between contexts that call for formal English (e.g., presenting ideas) and situations where informal discourse is appropriate (e.g., small-group discussion).

#### **Vocabulary Acquisition and Use**

- L.4.4. Determine or clarify the meaning of unknown and multiple-meaning words and phrases based on *grade 4 reading and content*, choosing flexibly from a range of strategies.
  - Use context (e.g., definitions, examples, or restatements in text) as a clue to the meaning of a word or phrase.
  - Use common, grade-appropriate Greek and Latin affixes and roots as clues to the meaning of a word (e.g., *telegraph*, *photograph*, *autograph*).
  - Consult reference materials (e.g., dictionaries, glossaries, thesauruses), both print and digital, to find the pronunciation and determine or clarify the precise meaning of key words and phrases.
- L.4.5. Demonstrate understanding of figurative language, word relationships, and nuances in word meanings.
  - Explain the meaning of simple similes and metaphors (e.g., as pretty as a picture) in context.
  - Recognize and explain the meaning of common idioms, adages, and proverbs.
  - Demonstrate understanding of words by relating them to their opposites (antonyms) and to words with similar but not identical meanings (synonyms).
- L.4.6. Acquire and use accurately grade-appropriate general academic and domain-specific words and phrases, including those that signal precise actions, emotions, or states of being (e.g., *quizzed*, *whined*, *stammered*) and that are basic to a particular topic (e.g., *wildlife*, *conservation*, and *endangered* when discussing animal preservation).

#### **ELA Standards – Grade 5**

#### **Reading Standards for Literature**

#### **Key Ideas and Details**

- RL.5.1. Quote accurately from a text when explaining what the text says explicitly and when drawing inferences from the text.
- RL.5.2. Determine a theme of a story, drama, or poem from details in the text, including how characters in a story or drama respond to challenges or how the speaker in a poem reflects upon a topic; summarize the text.
- RL.5.3. Compare and contrast two or more characters, settings, or events in a story or drama, drawing on specific details in the text (e.g., how characters interact).

#### **Craft and Structure**

- RL.5.4. Determine the meaning of words and phrases as they are used in a text, including figurative language such as metaphors and similes.
- RL.5.5. Explain how a series of chapters, scenes, or stanzas fits together to provide the overall structure of a particular story, drama, or poem.
- RL.5.6. Describe how a narrator's or speaker's point of view influences how events are described.

#### Integration of Knowledge and Ideas

- RL.5.7. Analyze how visual and multimedia elements contribute to the meaning, tone, or beauty of a text (e.g., graphic novel, multimedia presentation of fiction, folktale, myth, poem).
- RL.5.9. Compare and contrast stories in the same genre (e.g., mysteries and adventure stories) on their approaches to similar themes and topics.

#### Range of Reading and Level of Text Complexity

RL.5.10. By the end of the year, read and comprehend literature, including stories, dramas, and poetry, at the high end of the grades 4–5 text complexity band independently and proficiently.

## **Reading Standards for Informational Text**

#### **Key Ideas and Details**

- RI.5.1. Quote accurately from a text when explaining what the text says explicitly and when drawing inferences from the text.
- RI.5.2. Determine two or more main ideas of a text and explain how they are supported by key details; summarize the text.
- RI.5.3. Explain the relationships or interactions between two or more individuals, events, ideas, or concepts in a historical, scientific, or technical text based on specific information in the text.

#### **Craft and Structure**

- RI.5.4. Determine the meaning of general academic and domain-specific words and phrases in a text relevant to a *grade 5 topic or subject area*.
- RI.5.5. Compare and contrast the overall structure (e.g., chronology, comparison, cause/effect, problem/solution) of events, ideas, concepts, or information in two or more texts.
- RI.5.6. Analyze multiple accounts of the same event or topic, noting important similarities and differences in the point of view they represent.

#### Integration of Knowledge and Ideas

- RI.5.7. Draw on information from multiple print or digital sources, demonstrating the ability to locate an answer to a question quickly or to solve a problem efficiently.
- RI.5.8. Explain how an author uses reasons and evidence to support particular points in a text, identifying which reasons and evidence support which point(s).
- RI.5.9. Integrate information from several texts on the same topic in order to write or speak about the subject knowledgeably.

#### Range of Reading and Level of Text Complexity

RI.5.10. By the end of the year, read and comprehend informational texts, including history/social studies, science, and technical texts, at the high end of the grades 4–5 text complexity band independently and proficiently.

## Reading Standards: Foundational Skills

#### **Phonics and Word Recognition**

RF.5.3. Know and apply grade-level phonics and word analysis skills in decoding words.

• Use combined knowledge of all letter-sound correspondences, syllabication patterns, and morphology (e.g., roots and affixes) to read accurately unfamiliar multisyllabic words in context and out of context.

#### Fluency

RF.5.4. Read with sufficient accuracy and fluency to support comprehension.

- Read on-level text with purpose and understanding.
- Read on-level prose and poetry orally with accuracy, appropriate rate, and expression on successive readings.
- Use context to confirm or self-correct word recognition and understanding, rereading as necessary.

### **Writing Standards**

#### **Text Types and Purposes**

- W.5.1. Write opinion pieces on topics or texts, supporting a point of view with reasons and information.
  - Introduce a topic or text clearly, state an opinion, and create an organizational structure in which ideas are logically grouped to support the writer's purpose.
  - Provide logically ordered reasons that are supported by facts and details.
  - Link opinion and reasons using words, phrases, and clauses (e.g., consequently, specifically).
  - Provide a concluding statement or section related to the opinion presented.
- W.5.2. Write informative/explanatory texts to examine a topic and convey ideas and information clearly.
  - Introduce a topic clearly, provide a general observation and focus, and group related information logically; include formatting (e.g., headings), illustrations, and multimedia when useful to aiding comprehension.
  - Develop the topic with facts, definitions, concrete details, quotations, or other information and examples related to the topic.
  - Link ideas within and across categories of information using words, phrases, and clauses (e.g., in contrast, especially).
  - Use precise language and domain-specific vocabulary to inform about or explain the topic.
  - Provide a concluding statement or section related to the information or explanation presented.
- W.5.3. Write narratives to develop real or imagined experiences or events using effective technique, descriptive details, and clear event sequences.
  - Orient the reader by establishing a situation and introducing a narrator and/or characters; organize an event sequence that unfolds naturally.
  - Use narrative techniques, such as dialogue, description, and pacing, to develop experiences and events or show the responses of characters to situations.
  - Use a variety of transitional words, phrases, and clauses to manage the sequence of events.
  - Use concrete words and phrases and sensory details to convey experiences and events precisely.
  - Provide a conclusion that follows from the narrated experiences or events.

#### **Production and Distribution of Writing**

- W.5.4. Produce clear and coherent writing in which the development and organization are appropriate to task, purpose, and audience.
- W.5.5. With guidance and support from peers and adults, develop and strengthen writing as needed by planning, revising, editing, rewriting, or trying a new approach.
- W.5.6. With some guidance and support from adults, use technology, including the Internet, to produce and publish writing as well as to interact and collaborate with others; demonstrate sufficient command of keyboarding skills to type a minimum of two pages in a single sitting.

#### Research to Build and Present Knowledge

- W.5.7. Conduct short research projects that use several sources to build knowledge through investigation of different aspects of a topic.
- W.5.8. Recall relevant information from experiences or gather relevant information from print and digital sources; summarize or paraphrase information in notes and finished work, and provide a list of sources.
- W.5.9. Draw evidence from literary or informational texts to support analysis, reflection, and research.
  - a. Apply *grade 5 Reading standards* to literature (e.g., "Compare and contrast two or more characters, settings, or events in a story or a drama, drawing on specific details in the text [e.g., how characters interact]").
  - b. Apply *grade 5 Reading standards* to informational texts (e.g., "Explain how an author uses reasons and evidence to support particular points in a text, identifying which reasons and evidence support which point[s]").

#### Range of Writing

W.5.10. Write routinely over extended time frames (time for research, reflection, and revision) and shorter time frames (a single sitting or a day or two) for a range of discipline-specific tasks, purposes, and audiences.

## **Speaking and Listening Standards**

#### **Comprehension and Collaboration**

- SL.5.1. Engage effectively in a range of collaborative discussions (one-on-one, in groups, and teacher-led) with diverse partners on *grade 5 topics and texts*, building on others' ideas and expressing their own clearly.
  - Come to discussions prepared, having read or studied required material; explicitly draw on that preparation and other information known about the topic to explore ideas under discussion.
  - Follow agreed-upon rules for discussions and carry out assigned roles.
  - Pose and respond to specific questions by making comments that contribute to the discussion and elaborate on the remarks of others.
  - Review the key ideas expressed and draw conclusions in light of information and knowledge gained from the discussions.
- SL.5.2. Summarize a written text read aloud or information presented in diverse media and formats, including visually, quantitatively, and orally.
- SL.5.3. Summarize the points a speaker makes and explain how each claim is supported by reasons and evidence.

#### Presentation of Knowledge and Ideas

- SL.5.4. Report on a topic or text or present an opinion, sequencing ideas logically and using appropriate facts and relevant, descriptive details to support main ideas or themes; speak clearly at an understandable pace.
- SL.5.5. Include multimedia components (e.g., graphics, sound) and visual displays in presentations when appropriate to enhance the development of main ideas or themes.
- SL.5.6. Adapt speech to a variety of contexts and tasks, using formal English when appropriate to task and situation.

## **Language Standards**

#### **Conventions of Standard English**

- L.5.1. Demonstrate command of the conventions of standard English grammar and usage when writing or speaking.
  - Explain the function of conjunctions, prepositions, and interjections in general and their function in particular sentences.
  - Form and use the perfect (e.g., I had walked; I have walked; I will have walked) verb tenses.
  - Use verb tense to convey various times, sequences, states, and conditions.
  - Recognize and correct inappropriate shifts in verb tense.
  - Use correlative conjunctions (e.g., either/or, neither/nor).
- L.5.2. Demonstrate command of the conventions of standard English capitalization, punctuation, and spelling when writing.
  - Use punctuation to separate items in a series.
  - Use a comma to separate an introductory element from the rest of the sentence.
  - Use a comma to set off the words yes and no (e.g., Yes, thank you), to set off a tag question from the rest of the sentence (e.g., It's true, isn't it?), and to indicate direct address (e.g., Is that you, Steve?).
  - Use underlining, quotation marks, or italics to indicate titles of works.
  - Spell grade-appropriate words correctly, consulting references as needed.

#### **Knowledge of Language**

- L.5.3. Use knowledge of language and its conventions when writing, speaking, reading, or listening.
  - Expand, combine, and reduce sentences for meaning, reader/listener interest, and style.
  - Compare and contrast the varieties of English (e.g., dialects, registers) used in stories, dramas, or poems.

#### **Vocabulary Acquisition and Use**

- L.5.4. Determine or clarify the meaning of unknown and multiple-meaning words and phrases based on *grade 5 reading and content*, choosing flexibly from a range of strategies.
  - Use context (e.g., cause/effect relationships and comparisons in text) as a clue to the meaning of a word or phrase.
  - Use common, grade-appropriate Greek and Latin affixes and roots as clues to the meaning of a word (e.g., *photograph*, *photosynthesis*).
  - Consult reference materials (e.g., dictionaries, glossaries, thesauruses), both print and digital, to find the pronunciation and determine or clarify the precise meaning of key words and phrases.
- L.5.5. Demonstrate understanding of figurative language, word relationships, and nuances in word meanings.
  - Interpret figurative language, including similes and metaphors, in context.
  - Recognize and explain the meaning of common idioms, adages, and proverbs.
  - Use the relationship between particular words (e.g., synonyms, antonyms, homographs) to better understand each of the words.
- L.5.6. Acquire and use accurately grade-appropriate general academic and domain-specific words and phrases, including those that signal contrast, addition, and other logical relationships (e.g., however, although, nevertheless, similarly, moreover, in addition).



## **Measuring Text Complexity**

#### Qualitative evaluation of the text

 Levels of meaning, structure, language conventionality and clarity, and knowledge demands

#### Quantitative evaluation of the text

• Readability measures and other scores of text complexity

#### Matching reader to text and task

 Reader variables (such as motivation, knowledge, and experiences) and task variables (such as purpose and the complexity generated by the task assigned and the questions posed)

Students in K–5 apply the Reading standards to the following range of text types, with texts selected from a broad range of cultures and periods.

| Literature                                                                                                       |                                                    |                                                                                                | Informational Text                                                                                                                                                                                                                                 |
|------------------------------------------------------------------------------------------------------------------|----------------------------------------------------|------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Stories                                                                                                          | Dramas                                             | Poetry                                                                                         | Literary Nonfiction and Historical, Scientific, and Technical Texts                                                                                                                                                                                |
| Includes children's adventure<br>stories, folktales, legends,<br>fables, fantasy, realistic fiction,<br>and myth | Includes staged dialogue and brief familiar scenes | Includes nursery rhymes and the subgenres of the narrative poem, limerick, and free verse poem | Includes biographies and autobiographies; books about history, social studies, science, and the arts; technical texts, including directions, forms, and information displayed in graphs, charts, or maps; and digital sources on a range of topics |

## Texts Illustrating the Complexity, Quality, & Range of Student Reading 2-5

|     | Literature: Stories, Drama, Poetry                                                                                                                                                                                                                                                                                           | Informational Texts: Literary Nonfiction and Historical, Scientific, and Technical Texts                                                                                                                                                                                                                                                                                     |
|-----|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 2-3 | <ul> <li>Who Has Seen the Wind?" by Christina G. Rossetti (1893)</li> <li>Charlotte's Web by E. B. White (1952)*</li> <li>Sarah, Plain and Tall by Patricia MacLachlan (1985)</li> <li>Tops and Bottoms by Janet Stevens (1995)</li> <li>Poppleton in Winter by Cynthia Rylant, illustrated by Mark Teague (2001)</li> </ul> | <ul> <li>A Medieval Feast by Aliki (1983)</li> <li>From Seed to Plant by Gail Gibbons (1991)</li> <li>The Story of Ruby Bridges by Robert Coles (1995)*</li> <li>A Drop of Water: A Book of Science and Wonder by Walter Wick (1997)</li> <li>Moonshot: The Flight of Apollo 11 by Brian Floca (2009)</li> </ul>                                                             |
| 4-5 | <ul> <li>Alice's Adventures in Wonderland by Lewis Carroll (1865)</li> <li>"Casey at the Bat" by Ernest Lawrence Thayer (1888)</li> <li>The Black Stallion by Walter Farley (1941)</li> <li>"Zlateh the Goat" by Isaac Bashevis Singer (1984)</li> <li>Where the Mountain Meets the Moon by Grace Lin (2009)</li> </ul>      | <ul> <li>Discovering Mars: The Amazing Story of the Red Planet by Melvin Berger (1992)</li> <li>Hurricanes: Earth's Mightiest Storms by Patricia Lauber (1996)</li> <li>A History of US by Joy Hakim (2005)</li> <li>Horses by Seymour Simon (2006)</li> <li>Quest for the Tree Kangaroo: An Expedition to the Cloud Forest of New Guinea by Sy Montgomery (2006)</li> </ul> |

#### Note:

Given space limitations, the illustrative texts listed above are meant only to show individual titles that are representative of a wide range of topics and genres. (See Appendix B of the Common Core Standards for excerpts of these and other texts illustrative of K–5 text complexity, quality, and range.) At a curricular or instructional level, within and across grade levels, texts need to be selected around topics or themes that generate knowledge and allow students to study those topics or themes in depth. On the next page is an **example** of progressions of texts building knowledge across grade levels.

## Staying on Topic Within a Grade & Across Grades

Building knowledge systematically in English language arts is like giving children various pieces of a puzzle in each grade that, over time, will form one big picture. At a curricular or instructional level, texts—within and across grade levels—need to be selected around topics or themes that systematically develop the knowledge base of students. Within a grade level, there should be an adequate number of titles on a single topic that would allow children to study that topic for a sustained period. The knowledge children have learned about particular topics in early grade levels should then be expanded and developed in subsequent grade levels to ensure an increasingly deeper understanding of these topics. Children in the upper elementary grades will generally be expected to read these texts independently and reflect on them in writing. However, children in the early grades (particularly K-2) should participate in rich, structured conversations with an adult in response to the written texts that are read aloud, orally comparing and contrasting as well as analyzing and synthesizing, in the manner called for by the Standards.

Preparation for reading complex informational texts should begin at the very earliest elementary school grades. What follows is one example that uses domain-specific nonfiction titles across grade levels to illustrate how curriculum designers and classroom teachers can infuse the English language arts block with rich, age-appropriate content knowledge and vocabulary in history/social studies, science, and the arts. Having students listen to informational read-alouds in the early grades helps lay the necessary foundation for students' reading and understanding of increasingly complex texts on their own in subsequent grades.

This is only a sample. Full chart can be found on Standards web site.

| Exemplar Texts<br>on a Topic<br>Across Grades                      | 2-3                                                                 | 4-5                                                     |
|--------------------------------------------------------------------|---------------------------------------------------------------------|---------------------------------------------------------|
| The Human Body                                                     | Digestive and excretory systems                                     | Circulatory system                                      |
| Students can begin learning about the human body                   | What Happens to a Hamburger by Paul Showers (1985)                  | <i>The Heart</i> by Seymour Simon (2006)                |
| starting in<br>kindergarten and<br>then review and<br>extend their | The Digestive System by Christine Taylor-Butler (2008)              | The Heart and<br>Circulation by Carol<br>Ballard (2005) |
| learning during each subsequent grade.                             | The Digestive System by Rebecca L. Johnson (2006)                   | The Circulatory System by Kristin Petrie (2007)         |
|                                                                    | The Digestive System by Kristin Petrie (2007)                       | The Amazing Circulatory System by John Burstein         |
|                                                                    | Muscular, skeletal, and nervous systems                             | (2009)                                                  |
|                                                                    | ľ                                                                   | Respiratory system                                      |
|                                                                    | The Mighty Muscular and Skeletal Systems Crabtree Publishing (2009) | The Lungs by Seymour Simon (2007)                       |
|                                                                    | Muscles by Seymour Simon (1998)                                     | The Respiratory System by Susan Glass (2004)            |
|                                                                    | Bones by Seymour Simon (1998)                                       | Endocrine system                                        |
|                                                                    | The Nervous System by Joelle Riley (2004)                           | The Endocrine System by Rebecca Olien (2006)            |

# Implementation Guide – Grade 4 ELA

#### **COMMON CORE STANDARDS: ELA**

Implementing the Common Core Standards may seem to be a daunting task, however, the ELA Curriculum Committee has created four sample guidelines/templates to introduce you to the standards. We have provided a guideline for each of the four types of writing prescribed for each grade. You will see that we have correlated Reading Standards with each Writing piece. These guidelines are meant to be a starting point and while they are comprehensive they do not include every standard. Our intent is that teachers will plug-in other standards as needed. The book companies have created correlations to the Common Core Standards so you will have them to use as well, and you will have the flexibility to add ELA standards from each category (Reading, Writing, Speaking and Listening, and Language) depending on the theme or story.

Coding: ELA.4.A.1 refers to English Language Arts – Grade 4 Topic A – Skill 1

Reading Standards: ELA.4.G- Integration

| Grade 4                                   | "Why Should Philadelphia Be the Capital of Pennsylvania?" | of Knowledge and Ideas                            |
|-------------------------------------------|-----------------------------------------------------------|---------------------------------------------------|
| Γ=                                        |                                                           |                                                   |
| Essential                                 | What is an <i>opinion</i> ?                               |                                                   |
| <b>Questions</b> What should I be able to | What is a fact?                                           | How do we distinguish the difference between fact |
| answer?<br>What guides my                 | How will I write an opinion piece?                        | and interpretation?                               |
| thinking?                                 | How do I write a letter to the editor?                    | How do I interpret information from different     |
|                                           | What do I include in an opinion piece of writing?         | sources on the same topic?                        |
|                                           | What kind of words do I use to link reasons and           |                                                   |
|                                           | opinions?                                                 |                                                   |

Writing Standards: ELA.4.K – Text Type and

**Opinion** 

| Assessment                                       | Writing rubric for letter to the editor                  | Read news articles/editorial pages – discuss and   |
|--------------------------------------------------|----------------------------------------------------------|----------------------------------------------------|
| What will I be expected to know, understand, and | Graphic organizer showing opinion and supporting         | write summaries                                    |
| be able to do in order to demonstrate my         | details                                                  | Use online sources (blogs, news magazines, etc.)   |
| learning?                                        | Peer review and editing                                  | - discuss and summarize                            |
|                                                  | Completed letter to the editor                           |                                                    |
| Skills                                           | K.1- Write an information piece on topic, supporting a   | G.7 – Interpret information presented visually,    |
| What skills do I need to have in order to answer | point of view with reasons and information.              | orally, or quantitatively and explain how the      |
| the essential questions?                         | L.4 – Produce clear and coherent writing in which the    | information contributes to an understanding of the |
|                                                  | development and organization are appropriate to task,    | text in which it appears                           |
|                                                  | purpose, and audience                                    |                                                    |
|                                                  | L.5- Develop and strengthen writing by planning,         | G.8 – Explain how the author uses reasons and      |
|                                                  | revising, and editing                                    | evidence to support particular points in a text    |
|                                                  | L.6 – Use technology to produce and publish writing as   |                                                    |
|                                                  | well as interact and collaborate with others;            | G.9 – Integrate information from two texts on the  |
|                                                  | demonstrate sufficient command of keyboarding skills     | same topic in order to write or speak about the    |
|                                                  | M.9 – Draw evidence from literary or informational texts | subject                                            |
|                                                  | to support analysis, reflection, and research            |                                                    |
|                                                  | Q.1 – Demonstrate command of the conventions of          | O.1 – Engage effectively in a range of             |
|                                                  | standard English grammar and usage when writing          | collaborative discussions with diverse partners,   |
|                                                  | Q.2 – Demonstrate command of the conventions of          | building on others' ideas and expressing their own |
|                                                  | standard English capitalization, punctuation, and        | clearly                                            |
|                                                  | spelling when writing                                    |                                                    |
|                                                  | R.3 .C – Differentiate between contexts that call for    |                                                    |
|                                                  | formal English and situations where informal discourse   |                                                    |

|                                                                                                  | is appropriate                                                                                                                                |       |                                        |
|--------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------|-------|----------------------------------------|
|                                                                                                  | S.6 – Acquire and use accurately grade-appropriate                                                                                            |       |                                        |
|                                                                                                  | general academic and domain-specific words and                                                                                                |       |                                        |
|                                                                                                  | phrases, including those that signal precise actions,                                                                                         |       |                                        |
|                                                                                                  | emotions, or states of being and that are basic to a                                                                                          |       |                                        |
|                                                                                                  | particular topic                                                                                                                              |       |                                        |
| Content What content do I need                                                                   | Writing Informational piece                                                                                                                   | •     | Summarizing                            |
| to know in order to<br>answer the essential<br>questions?                                        | Fact/Opinion                                                                                                                                  | •     | Supporting details                     |
| Integration of Learning How does this learning connect to my other areas (subjects) of learning? | Social Studies (above) Technology:  • Use of technology tools to create a graphic organizer  • Use the computer to write, revise, and publish |       |                                        |
| Tools for Learning                                                                               | Digital resources –Search engines; Internet web sites                                                                                         |       |                                        |
| Which tools will I use that will assist me in my learning?                                       | Reference materials – Use of atlas                                                                                                            |       |                                        |
|                                                                                                  | Primary sources – Interviews: Governor's office,                                                                                              |       |                                        |
|                                                                                                  | Mayors' offices                                                                                                                               |       |                                        |
| Which 21 <sup>st</sup> Century Skills a                                                          | re woven into this standard? Critical Thinking/Problem SolvinCommunications                                                                   | ng    | Collaboration<br>Creativity/Innovation |
| What level of rigor will I be                                                                    | using? (A, C) What level of relevance will I be using?                                                                                        | (B,D) |                                        |

|   | Narrative - | Writing Standards: ELA.4.J.3 – Writing                                                  | Reading Standards: ELA.4.A – Key Ideas |
|---|-------------|-----------------------------------------------------------------------------------------|----------------------------------------|
|   | Grade 4     | Narratives                                                                              | and Details                            |
|   |             | Write a story about the "The First 4 <sup>th</sup> of July Celebration in Philadelphia" | ELA.4.B – Craft and Structure          |
| L |             | Philadelphia                                                                            |                                        |

| Essential                                          | What/who is a narrator and what is his role in a           | How do I determine a theme of a narrative?            |
|----------------------------------------------------|------------------------------------------------------------|-------------------------------------------------------|
|                                                    | What who is a harrator and what is his fole in a           | riow do i determine a theme of a namative:            |
| Questions What should I be able to                 | narrative?                                                 | How do I use specific details in the text to describe |
| answer?<br>What guides my                          | How do I select and establish a situation for a narrative? | in depth a character, setting, or event in a          |
| thinking?                                          | How do I introduce characters into a narrative?            | narrative story?                                      |
|                                                    | How do I use dialogue and descriptions to develop the      |                                                       |
|                                                    | experiences and events?                                    | How is a narrative different from poems, drama,       |
|                                                    | What transitional words and phrases do I use to            | etc.?                                                 |
|                                                    | manage the sequence of events?                             |                                                       |
|                                                    | How do I use concrete and phrases and sensory details      |                                                       |
|                                                    | to convey experiences and events precisely?                |                                                       |
|                                                    | How do I write a conclusion that follows from the          |                                                       |
|                                                    | narrated experiences or events?                            |                                                       |
| Assessment                                         | Use a writing rubric specific to narratives                | Partner reading of narratives                         |
| What will I be expected to know, understand, and   | Use a character to web to develop story characters         | Describe in depth a character, setting, or event in   |
| be able to do in order to demonstrate my learning? |                                                            | a story                                               |

| Skills                                           | K.3.a Orient the reader by establishing a situation and   | A.3. Describe in depth a character, setting, or     |
|--------------------------------------------------|-----------------------------------------------------------|-----------------------------------------------------|
| What skills do I need to have in order to answer | introducing a narrator and/or characters, organize an     | event                                               |
| the essential questions?                         | event sequence and unfolds naturally                      | B.6 Compare and contrast the point of view from     |
|                                                  |                                                           | which different stories are narrated, including the |
|                                                  | K.3.b Use dialogue and description to develop             | difference between first- and third- person         |
|                                                  | experiences and events or show the responses of           | narrations                                          |
|                                                  | characters to sitations                                   | F.6 Compare and contrast a firsthand and            |
|                                                  | K.3.c Use a variety of transitional words and phrases to  | secondhand account of the same event or topic       |
|                                                  | manage the sequence of events                             |                                                     |
|                                                  | K.3.d Use concrete words and phrases and sensory          |                                                     |
|                                                  | details to convey experiences and events precisely        |                                                     |
|                                                  | K.3.e Provide a conclusion that follows from the          |                                                     |
|                                                  | narrated experiences or events                            |                                                     |
|                                                  | Q.1.a Use relative pronouns and relative adverbs          |                                                     |
|                                                  | Q. 2.a Use correct capitalization                         |                                                     |
|                                                  | Q.2.b Use commas, and quotation marks to mark direct      |                                                     |
|                                                  | speech and quotations from a text                         |                                                     |
|                                                  | R.3.c Differentiate between contexts that call for formal |                                                     |
|                                                  | English and situations that where informal discourse is   |                                                     |
|                                                  | appropriate                                               |                                                     |

S.5.b Recognize and explain the meaning of common

idioms, adages, and proverbs

| Content                                           | Research skills                                          | How to Read for information                    |
|---------------------------------------------------|----------------------------------------------------------|------------------------------------------------|
| What content do I need to know in order to        | Note taking                                              | How to establish setting                       |
| answer the essential questions?                   | Writing process                                          |                                                |
|                                                   | How to write quotation, dialogues                        |                                                |
| Integration of                                    | Social Studies:                                          | Reading biographies for background information |
| Learning How does this learning                   | Historical persons of time period                        |                                                |
| connect to my other areas (subjects) of learning? | Characteristics of the time period                       |                                                |
|                                                   | Technology:                                              |                                                |
|                                                   | Use of search engines                                    |                                                |
|                                                   | How to use links on web sites                            |                                                |
|                                                   | Keyboard- Work processing skills; clipart; use of        |                                                |
|                                                   | photos                                                   |                                                |
| Tools for Learning                                | Library – Non-fiction and reference sections; historical | Sample narratives                              |
| Which tools will I use that will assist me in my  | fiction                                                  | Picture books                                  |
| learning?                                         | Search engines, Internet – websites                      |                                                |
|                                                   | Graphic organizers (Inspiration software)                |                                                |
|                                                   |                                                          |                                                |

Which 21<sup>st</sup> Century Skills are woven into this standard? \_\_Critical Thinking/Problem Solving \_\_Communications \_\_Creativity/Innovation What level of rigor will I be using? (A, C)\_\_\_\_ What level of relevance will I be using?\_\_\_\_ (B,D)

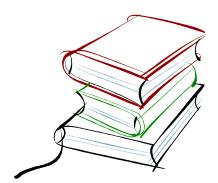
| Informational<br>Writing –<br>Grade 4 | Writing Standards: ELA.4.J.2 – Informative/Explanatory Compare and contrast regions in Pennsylvania | Reading Standards: ELA.4.F – Craft And Structure |
|---------------------------------------|-----------------------------------------------------------------------------------------------------|--------------------------------------------------|
| Essential                             |                                                                                                     |                                                  |

| Essential                                        |                                                          |                                                  |
|--------------------------------------------------|----------------------------------------------------------|--------------------------------------------------|
| <b>Questions</b> What should I be able to        | How do I introduce my topic clearly?                     | What specific words should I use about my topic? |
| answer?<br>What guides my                        | How do I develop my topic?                               | What structure should I use (chronology,         |
| thinking?                                        | What kinds of words and phrases do I use to link my      | cause/effect,                                    |
|                                                  | ideas?                                                   | compare/contrast, problem/solution)?             |
|                                                  | What precise vocabulary and language should I use?       | How do I evaluate information sources?           |
|                                                  | How do I write a concluding statement?                   |                                                  |
|                                                  |                                                          |                                                  |
|                                                  |                                                          |                                                  |
| Assessment                                       | Use of writing rubric                                    | Read some samples of informative/explanatory     |
| What will I be expected to know, understand, and | Compare and contrast regions in Pennsylvania -           | writing in magazines, newspapers, and web sites  |
| be able to do in order to demonstrate my         | Outline or graphic organizer                             | Use a rubric to determine a good sample          |
| learning?                                        | Peer review of introductory statements/paragraphs        |                                                  |
|                                                  | List topic-specific words/vocabulary                     |                                                  |
|                                                  | Peer editing of rough draft                              |                                                  |
|                                                  | Publish the written informative/explanatory piece (use a |                                                  |
|                                                  | rubric)                                                  |                                                  |

| Skills                                           | J.2.a Introduce a topic clearly                         | F.4 Determine the meaning of general academic        |
|--------------------------------------------------|---------------------------------------------------------|------------------------------------------------------|
| What skills do I need to                         | J.2.b Develop a topic with facts, definitions, related  | and domain-specific words and phrases in a text      |
| have in order to answer the essential questions? |                                                         | ·                                                    |
| ·                                                | to the topic                                            | relevant to a grade 4 topic or subject area          |
|                                                  | J.2.c Link ideas within categories of information       | F.5 Describe the overall structure of events,        |
|                                                  | J.2.d Use precise language and domain-specific          | ideas, concepts, or information in a text or part of |
|                                                  | vocabulary                                              | text                                                 |
|                                                  | J.2.e Provide a concluding statement or section related | F.6 Compare and contrast a firsthand and             |
|                                                  | to the information or explanation presented             | secondhand account of the same event or topic,       |
|                                                  |                                                         | describe the differences in focus and the            |
|                                                  |                                                         | information provided                                 |
| Content                                          | Research - Relevant information from multiple sources   | Using relevant information from multiple sources     |
| What content do I need to know in order to       | regions (maps, web sites, atlas, etc.)                  | on topic from content area                           |
| answer the essential questions?                  | Words, phrases, and graphics related to topic           |                                                      |
|                                                  | Linking words and phrases                               |                                                      |
| Integration of                                   | Social Studies:                                         | Library skills - Reference materials (print and      |
| Learning How does this learning                  | Examine the topic of Pennsylvania Regions               | online)                                              |
| connect to my other<br>areas (subjects) of       | Identify characteristics of each region                 |                                                      |
| learning?                                        | Technology:                                             |                                                      |
|                                                  | use of internet resources                               |                                                      |
|                                                  | presentation skills                                     |                                                      |
|                                                  | keyboard skills                                         |                                                      |

| Tools for Learning                               | Digital resources: Search engines; internet web sites | Textbooks, nonfiction materials |
|--------------------------------------------------|-------------------------------------------------------|---------------------------------|
| Which tools will I use that will assist me in my | Graphic organizers                                    |                                 |
| learning?                                        | Primary sources: Local governments/contacts           |                                 |

Which 21<sup>st</sup> Century Skills are woven into this standard? \_\_Critical Thinking/Problem Solving \_\_Communications \_\_Communications \_\_Creativity/Innovation What level of rigor will I be using? (A, C)\_\_ What level of relevance will I be using?\_\_ (B,D)



| Research –<br>Grade 4                                                                                          | Writing Standards: ELA.4.L – Research to Build and Present Knowledge                                                                                                                                                   | Reading Standards: ELA.4.F – Integration of Knowledge and Ideas                                                                                                                                                                       |
|----------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Essential Questions What should I be able to answer? What guides my thinking?                                  | How can I present knowledge about a specific topic as a short research report?  What print and digital resources are reliable to use?  How can I make and use notes to write a report?  How do I reference my sources? | How do I interpret information presented visually, orally, or quantitatively and explain how the information contributes to an understanding of text?  How do I integrate information from different texts/sources on the same topic? |
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Take notes on note cards Organize information List sources Use details to support points                                                                                                                               | Read for information                                                                                                                                                                                                                  |

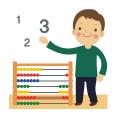


| Skills What skills do I need to have in order to answer the essential questions?                 | 4.L.7 conduct short research projects                     | 4.F.7 Interpret information                                 |
|--------------------------------------------------------------------------------------------------|-----------------------------------------------------------|-------------------------------------------------------------|
|                                                                                                  | 4. L.8 gather information from print and digital sources; | 4.F.8 Explain how an author uses reasons and                |
|                                                                                                  | categorize information                                    | evidence to support particular points                       |
|                                                                                                  | 4.L.9.a draw evidence from literary or informational      | 4.F.9 Integrate information from two texts on the           |
|                                                                                                  | texts to support analysis, reflection, and research       | same topic in order to write or speak about the             |
|                                                                                                  | 4.L.9.b Explain how an author uses reasons and            | subject knowledgeably.                                      |
|                                                                                                  | evidence to support particular points in text             |                                                             |
| Content What content do I need to know in order to answer the essential questions?               | Write a short research report                             | Main Ideas and details of a text                            |
|                                                                                                  | Select good resources (print and digital)                 | Describe in depth a character or event                      |
|                                                                                                  | Organize information and write an outline                 | Compare and contrast a firsthand and                        |
|                                                                                                  | Create a visual presentation (i.e. Power Point, poster,   | secondhand account of the same event or topic               |
|                                                                                                  | feature article))                                         |                                                             |
| Integration of Learning How does this learning connect to my other areas (subjects) of learning? | Use Technology to research, produce and publish           | Choose informational text about a Science topic             |
|                                                                                                  | writings as well as to interact and collaborate with      | and write a short article for <i>Scholastic</i> magazine or |
|                                                                                                  | others on the same topic.                                 | create a Power Point presentation.                          |
|                                                                                                  | Compare the information from primary source               |                                                             |
|                                                                                                  | documents with the secondary sources                      |                                                             |
|                                                                                                  |                                                           |                                                             |
|                                                                                                  |                                                           |                                                             |

| Tools for Learning Which tools will I use that will assist me in my learning?                                                                                                                                                                        | Use of Noodle tools for gathering information and sources  Multimedia print  Encyclopedia, web 2.0  Primary sources depending on the topic given | Digital resources Reference materials Primary sources |  |  |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------|--|--|
| Which 21 <sup>st</sup> Century Skills are woven into this standard? Critical Thinking/Problem Solving Collaboration Communications Creativity/Innovation  What level of rigor will I be using? (A, C) What level of relevance will I be using? (B,D) |                                                                                                                                                  |                                                       |  |  |

# Mathematics

# **Grade 4**



Common Core State Standards – GradeThree

Common Core State Standards – Grade Four

Common Core State Standards – Grade Five

Implementation Guide – Grade Four

# **Key Points In Mathematics**

- The K-5 standards provide students with a solid foundation in whole numbers, addition, subtraction, multiplication, division, fractions and decimals—which help young students build the foundation to successfully apply more demanding math concepts and procedures, and move into applications.
- In kindergarten, the standards follow successful international models and recommendations from the National Research Council's Early Math Panel report, by focusing kindergarten work on the number core: learning how numbers correspond to quantities, and learning how to put numbers together and take them apart (the beginnings of addition and subtraction).
- The K-5 standards build on the best state standards to provide detailed guidance to teachers on how to navigate their way through knotty topics such as *fractions*, *negative numbers*, *and geometry*, and do so by maintaining a continuous progression from grade to grade.
- The standards stress not only procedural skill but also conceptual understanding, to make sure students are learning and
  absorbing the critical information they need to succeed at higher levels rather than the current practices by which many
  students learn enough to get by on the next test, but forget it shortly thereafter, only to review again the following year.
- Having built a strong foundation K-5, students can do hands on learning in geometry, algebra and probability and statistics. Students who have completed 7th grade and mastered the content and skills through the 7th grade will be *well-prepared for algebra* in grade 8.
- The middle school standards are robust and provide a coherent and rich *preparation for high school mathematics*.
- The high school standards call on students to *practice applying mathematical ways of thinking to real world issues and challenges*; they prepare students to think and reason mathematically.
- The high school standards set a *rigorous definition of college and career readiness*, by helping students develop a depth of understanding and ability to apply mathematics to novel situations, as college students and employees regularly do.
- The high school standards *emphasize mathematical modeling*, the use of mathematics and statistics to analyze empirical situations, understand them better, and improve decisions. For example, the standards state: Modeling links classroom mathematics and statistics to everyday life, work, and decision-making. It is the process of choosing and using appropriate mathematics and statistics to analyze empirical situations, to understand them better, and to improve decisions. Quantities and their relationships in physical, economic, public policy, social and everyday situations can be modeled using mathematical and statistical methods. When making mathematical models, technology is valuable for varying assumptions, exploring consequences, and comparing predictions with data.

#### **Standards for Mathematical Practice**

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. These practices rest on important "processes and proficiencies" with longstanding importance in mathematics education. The first of these are the NCTM process standards of problem solving, reasoning and proof, communication, representation, and connections. The second are the strands of mathematical proficiency specified in the National Research Council's report *Adding It Up*: adaptive reasoning, strategic competence, conceptual understanding (comprehension of mathematical concepts, operations and relations), procedural fluency (skill in carrying out procedures flexibly, accurately, efficiently and appropriately), and productive disposition (habitual inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one's own efficacy).

#### 1 Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

#### 2 Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems\involving quantitative relationships: the ability to *decontextualize*—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents—and the ability to *contextualize*, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

#### 3 Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

#### 4 Model with mathematics.

Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a

student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

#### 5 Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

#### 6 Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

#### 7 Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see  $7 \times 8$  equals the well remembered  $7 \times 5 + 7 \times 3$ , in preparation for learning about the distributive property. In the expression  $x^2 + 9x + 14$ , older students can see the 14 as  $2 \times 7$  and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see 5 - 3(x - y)2 as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.

#### 8 Look for and express regularity in repeated reasoning.

Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through (1, 2) with slope 3, middle school students might abstract the equation (y - 2)/(x - 1) = 3. Noticing the regularity in the way terms cancel when expanding (x - 1)(x + 1),  $(x - 1)(x^2 + x + 1)$ , and  $(x - 1)(x^3 + x^2 + x + 1)$  might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

# Connecting the Standards for Mathematical Practice to the Standards for Mathematical Content

The Standards for Mathematical Practice describe ways in which developing student practitioners of the discipline of mathematics increasingly ought to engage with the subject matter as they grow in mathematical maturity and expertise throughout the elementary, middle and high school years. Designers of curricula, assessments, and professional development should all attend to the need to connect the mathematical practices to mathematical content in mathematics instruction.

The Standards for Mathematical Content are a balanced combination of procedure and understanding. Expectations that begin with the word "understand" are often especially good opportunities to connect the practices to the content. Students who lack understanding of a topic may rely on procedures too heavily. Without a flexible base from which to work, they may be less likely to consider analogous problems, represent problems coherently, justify conclusions, apply the mathematics to practical situations, use technology mindfully to work with the mathematics, explain the mathematics accurately to other students, step back for an overview, or deviate from a known procedure to find a shortcut. In short, a lack of understanding effectively prevents a student from engaging in the mathematical practices. In this respect, those content standards which set an expectation of understanding are potential "points of intersection" between the Standards for Mathematical Content and the Standards for Mathematical Practice. These points of intersection are intended to be weighted toward central and generative concepts in the school mathematics curriculum that most merit the time, resources, innovative energies, and focus necessary to qualitatively improve the curriculum, instruction, assessment, professional development, and student achievement in mathematics.



### **Mathematics Standards**

#### Grade 3

In Grade 3, instructional time should focus on four critical areas: (1) developing understanding of multiplication and division and strategies for multiplication and division within 100; (2) developing understanding of fractions, especially unit fractions (fractions with numerator 1); (3) developing understanding of the structure of rectangular arrays and of area; and (4) describing and analyzing two-dimensional shapes.

- 1. Students develop an understanding of the meanings of multiplication and division of whole numbers through activities and problems involving equal-sized groups, arrays, and area models; multiplication is finding an unknown product, and division is finding an unknown factor in these situations. For equal-sized group situations, division can require finding the unknown number of groups or the unknown group size. Students use properties of operations to calculate products of whole numbers, using increasingly sophisticated strategies based on these properties to solve multiplication and division problems involving single-digit factors. By comparing a variety of solution strategies, students learn the relationship between multiplication and division.
- 2. Students develop an understanding of fractions, beginning with unit fractions. Students view fractions in general as being built out of unit fractions, and they use fractions along with visual fraction models to represent parts of a whole. Students understand that the size of a fractional part is relative to the size of the whole. For example, 1/2 of the paint in a small bucket could be less paint than 1/3 of the paint in a larger bucket, but 1/3 of a ribbon is longer than 1/5 of the same ribbon because when the ribbon is divided into 3 equal parts, the parts are longer than when the ribbon is divided into 5 equal parts. Students are able to use fractions to represent numbers equal to, less than, and greater than one. They solve problems that involve comparing fractions by using visual fraction models and strategies based on noticing equal numerators or denominators.
- 3. Students recognize area as an attribute of two-dimensional regions. They measure the area of a shape by finding the total number of same-size units of area required to cover the shape without gaps or overlaps, a square with sides of unit length being the standard unit for measuring area. Students understand that rectangular arrays can be decomposed into identical rows or into identical columns. By decomposing rectangles into rectangular arrays of squares, students connect area to multiplication, and justify using multiplication to determine the area of a rectangle.

4. Students describe, analyze, and compare properties of two-dimensional shapes. They compare and classify shapes by
their sides and angles, and connect these with definitions of shapes. Students also relate their fraction work to geometry by
expressing the area of part of a shape as a unit fraction of the whole.

#### **Grade 3 Overview**

#### Operations and Algebraic Thinking

- Represent and solve problems involving multiplication and division.
- o Understand properties of multiplication and the relationship between multiplication and division.
- Multiply and divide within 100.
- Solve problems involving the four operations, and identify and explain patterns in arithmetic.

#### Number and Operations in Base Ten

o Use place value understanding and properties of operations to perform multi-digit arithmetic.

#### Number and Operations—Fractions

o Develop understanding of fractions as numbers.

#### Measurement and Data

- o Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.
- Represent and interpret data.
- o Geometric measurement: understand concepts of area and relate area to multiplication and to addition.
- Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.

#### Geometry

Reason with shapes and their attributes.

#### **Grade 3**

# **Operations and Algebraic Thinking**

#### Represent and solve problems involving multiplication and division.

- 3.OA.1. Interpret products of whole numbers, e.g., interpret 5 × 7 as the total number of objects in 5 groups of 7 objects each. For example, describe a context in which a total number of objects can be expressed as 5 × 7.
- 3.OA.2. Interpret whole-number quotients of whole numbers, e.g., interpret 56 ÷ 8 as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. For example, describe a context in which a number of shares or a number of groups can be expressed as 56 ÷ 8.
- 3.OA.3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
- 3.OA.4. Determine the unknown whole number in a multiplication or division equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations  $8 \times ? = 48$ ,  $5 = \square \div 3$ ,  $6 \times 6 = ?$ .

#### Understand properties of multiplication and the relationship between multiplication and division.

- 3.OA.5. Apply properties of operations as strategies to multiply and divide. [Students need not use formal terms for these properties.] Examples: If  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known. (Commutative property of multiplication.)  $3 \times 5 \times 2$  can be found by  $3 \times 5 = 15$ , then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 = 30$ . (Associative property of multiplication.) Knowing that  $8 \times 5 = 40$  and  $8 \times 2 = 16$ , one can find  $8 \times 7$  as  $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$ . (Distributive property.)
- 3.OA.6. Understand division as an unknown-factor problem. For example, find 32 ÷ 8 by finding the number that makes 32 when multiplied by 8. Multiply and divide within 100.
  - 3.OA.7. Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that  $8 \times 5 = 40$ , one knows  $40 \div 5 = 8$ ) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers.

#### Solve problems involving the four operations, and identify and explain patterns in arithmetic.

- 3.OA.8. Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. [This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).]
- 3.OA.9. Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations. For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.

# **Number and Operations in Base Ten**

# Use place value understanding and properties of operations to perform multi-digit arithmetic. [A range of algorithms may be used.]

- 3.NBT.1. Use place value understanding to round whole numbers to the nearest 10 or 100.
- 3.NBT.2. Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
- 3.NBT.3. Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., 9 × 80, 5 × 60) using strategies based on place value and properties of operations.

### **Number and Operations—Fractions**

#### [Grade 3 expectations in this domain are limited to fractions with denominators 2, 3, 4, 6, and 8.]

#### Develop understanding of fractions as numbers.

- 3.NF.1. Understand a fraction 1/b as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction a/b as the quantity formed by a parts of size 1/b.
- 3.NF.2. Understand a fraction as a number on the number line; represent fractions on a number line diagram.
  - Represent a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size 1/b and that the endpoint of the part based at 0 locates the number 1/b on the number line.
  - Represent a fraction a/b on a number line diagram by marking off a lengths 1/b from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line.
- 3.NF.3. Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.
  - Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.
  - Recognize and generate simple equivalent fractions, e.g., 1/2 = 2/4, 4/6 = 2/3). Explain why the fractions are equivalent, e.g., by using a visual fraction model.
  - Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. Examples: Express 3 in the form 3 = 3/1; recognize that 6/1 = 6; locate 4/4 and 1 at the same point of a number line diagram.
  - Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model.

#### **Measurement and Data**

#### Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.

- 3.MD.1 Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.
- 3.MD.2. Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l). [Excludes compound units such as cm³ and finding the geometric volume of a container.] Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem. [Excludes multiplicative comparison problems (problems involving notions of "times as much"]

#### Represent and interpret data.

- 3.MD.3. Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step "how many more" and "how many less" problems using information presented in scaled bar graphs. For example, draw a bar graph in which each square in the bar graph might represent 5 pets.
- 3.MD.4. Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.

#### Geometric measurement: understand concepts of area and relate area to multiplication and to addition.

- 3.MD.5. Recognize area as an attribute of plane figures and understand concepts of area measurement.
  - A square with side length 1 unit, called "a unit square," is said to have "one square unit" of area, and can be used to measure area.
  - A plane figure which can be covered without gaps or overlaps by *n* unit squares is said to have an area of *n* square units.
- 3.MD.6. Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units).
- 3.MD.7. Relate area to the operations of multiplication and addition.
  - Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.
  - Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.
  - Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and b + c is the sum of  $a \times b$  and  $a \times c$ . Use area models to represent the distributive property in mathematical reasoning.
  - Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world problems.

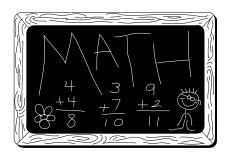
# Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.

3.MD.8. Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

# Geometry

#### Reason with shapes and their attributes.

- 3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.
- 3.G.2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. For example, partition a shape into 4 parts with equal area, and describe the area of each part as 1/4 of the area of the shape.



#### **Grade 4**

In Grade 4, instructional time should focus on three critical areas: (1) developing understanding and fluency with multi-digit multiplication, and developing understanding of dividing to find quotients involving multi-digit dividends; (2) developing an understanding of fraction equivalence, addition and subtraction of fractions with like denominators, and multiplication of fractions by whole numbers; (3) understanding that geometric figures can be analyzed and classified based on their properties, such as having parallel sides, perpendicular sides, particular angle measures, and symmetry.

- 1. Students generalize their understanding of place value to 1,000,000, understanding the relative sizes of numbers in each place. They apply their understanding of models for multiplication (equal-sized groups, arrays, area models), place value, and properties of operations, in particular the distributive property, as they develop, discuss, and use efficient, accurate, and generalizable methods to compute products of multi-digit whole numbers. Depending on the numbers and the context, they select and accurately apply appropriate methods to estimate or mentally calculate products. They develop fluency with efficient procedures for multiplying whole numbers; understand and explain why the procedures work based on place value and properties of operations; and use them to solve problems. Students apply their understanding of models for division, place value, properties of operations, and the relationship of division to multiplication as they develop, discuss, and use efficient, accurate, and generalizable procedures to find quotients involving multi-digit dividends. They select and accurately apply appropriate methods to estimate and mentally calculate quotients, and interpret remainders based upon the context.
- 2. Students develop understanding of fraction equivalence and operations with fractions. They recognize that two different fractions can be equal (e.g., 15/9 = 5/3), and they develop methods for generating and recognizing equivalent fractions. Students extend previous understandings about how fractions are built from unit fractions, composing fractions from unit fractions, decomposing fractions into unit fractions, and using the meaning of fractions and the meaning of multiplication to multiply a fraction by a whole number.
- 3. Students describe, analyze, compare, and classify two-dimensional shapes. Through building, drawing, and analyzing two-dimensional shapes, students deepen their understanding of properties of two-dimensional objects and the use of them to solve problems involving symmetry.

#### **Grade 4 Overview**

#### Operations and Algebraic Thinking

- Use the four operations with whole numbers to solve problems.
- Gain familiarity with factors and multiples.
- Generate and analyze patterns.

#### Number and Operations in Base Ten

- o Generalize place value understanding for multi-digit whole numbers.
- o Use place value understanding and properties of operations to perform multi-digit arithmetic

#### Number and Operations—Fractions

- Extend understanding of fraction equivalence and ordering.
- Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.
- o Understand decimal notation for fractions, and compare decimal fractions.

#### Measurement and Data

- Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.
- o Represent and interpret data.
- o Geometric measurement: understand concepts of angle and measure angles.

#### Geometry

o Draw and identify lines and angles, and classify shapes by properties of their lines and angles.

# **Operations and Algebraic Thinking**

#### Use the four operations with whole numbers to solve problems.

- 4.OA.1. Interpret a multiplication equation as a comparison, e.g., interpret 35 = 5 × 7 as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.
- 4.OA.2. Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.
- 4.OA.3. Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

#### Gain familiarity with factors and multiples.

4.OA.4. Find all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1–100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1–100 is prime or composite.

#### Generate and analyze patterns.

4.OA.5. Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. For example, given the rule "Add 3" and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.

# **Number and Operations in Base Ten**

[Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.]

#### Generalize place value understanding for multi-digit whole numbers.

- 4..NBT.1. Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. For example, recognize that 700 ÷ 70 = 10 by applying concepts of place value and division.
- 4..NBT.2. Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form. Compare two multi-digit numbers based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.
- 4..NBT.3. Use place value understanding to round multi-digit whole numbers to any place.

#### Use place value understanding and properties of operations to perform multi-digit arithmetic.

- 4..NBT.4. Fluently add and subtract multi-digit whole numbers using the standard algorithm.
- 4..NBT.5. Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.
- 4..NBT.6. Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.



# **Number and Operations—Fractions**

[Grade 4 expectations in this domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100.]

#### Extend understanding of fraction equivalence and ordering.

- 4.NF.1. Explain why a fraction a/b is equivalent to a fraction (n × a)/(n × b) by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.
- 4.NF.2. Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as 1/2. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model.

# Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.

- 4.NF.3. Understand a fraction a/b with a > 1 as a sum of fractions 1/b.
  - Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.
  - Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. Examples: 3/8 = 1/8 + 1/8 + 1/8 ; 3/8 = 1/8 + 2/8 ; 2 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8.
  - Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an
    equivalent fraction, and/or by using properties of operations and the relationship between addition and
    subtraction.
  - Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.

- 4.NF.4. Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.
  - Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to represent 5/4 as the product  $5 \times (1/4)$ , recording the conclusion by the equation  $5/4 = 5 \times (1/4)$ .
  - b. Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express 3 × (2/5) as 6 × (1/5), recognizing this product as 6/5. (In general, n × (a/b) = (n × a)/b.)
  - c. Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?

#### Understand decimal notation for fractions, and compare decimal fractions.

- 4.NF.5. Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. [Students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators in general. But addition and subtraction with unlike denominators in general is not a requirement at this grade.] For example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100.
- 4.NF.6. Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.
- 4.NF.7. Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual model.

#### **Measurement and Data**

# Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.

- 4.MD.1. Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a two-column table. For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36), ...
- 4.MD.2. Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.
- 4.MD.3. Apply the area and perimeter formulas for rectangles in real world and mathematical problems. For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor.

#### Represent and interpret data.

4.MD.4. Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Solve problems involving addition and subtraction of fractions by using information presented in line plots. For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection.

#### Geometric measurement: understand concepts of angle and measure angles.

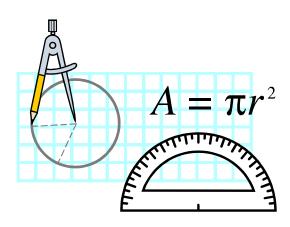
- 4.MD.5. Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle measurement:
  - An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through 1/360 of a circle is called a "one-degree angle," and can be used to measure angles.
  - An angle that turns through n one-degree angles is said to have an angle measure of n degrees.
- 4.MD.6. Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure.

4.MD.7. Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure.

# Geometry

#### Draw and identify lines and angles, and classify shapes by properties of their lines and angles.

- 4.G.1. Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures.
- 4.G.2. Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.
- 4.G.3. Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry.



#### **Grade 5**

In Grade 5, instructional time should focus on three critical areas: (1) developing fluency with addition and subtraction of fractions, and developing understanding of the multiplication of fractions and of division of fractions in limited cases (unit fractions divided by whole numbers and whole numbers divided by unit fractions); (2) extending division to 2-digit divisors, integrating decimal fractions into the place value system and developing understanding of operations with decimals to hundredths, and developing fluency with whole number and decimal operations; and (3) developing understanding of volume.

- 1. Students apply their understanding of fractions and fraction models to represent the addition and subtraction of fractions with unlike denominators as equivalent calculations with like denominators. They develop fluency in calculating sums and differences of fractions, and make reasonable estimates of them. Students also use the meaning of fractions, of multiplication and division, and the relationship between multiplication and division to understand and explain why the procedures for multiplying and dividing fractions make sense. (Note: this is limited to the case of dividing unit fractions by whole numbers and whole numbers by unit fractions.)
- 2. Students develop understanding of why division procedures work based on the meaning of base-ten numerals and properties of operations. They finalize fluency with multi-digit addition, subtraction, multiplication, and division. They apply their understandings of models for decimals, decimal notation, and properties of operations to add and subtract decimals to hundredths. They develop fluency in these computations, and make reasonable estimates of their results. Students use the relationship between decimals and fractions, as well as the relationship between finite decimals and whole numbers (i.e., a finite decimal multiplied by an appropriate power of 10 is a whole number), to understand and explain why the procedures for multiplying and dividing finite decimals make sense. They compute products and quotients of decimals to hundredths efficiently and accurately.
- 3. Students recognize volume as an attribute of three-dimensional space. They understand that volume can be measured by finding the total number of same-size units of volume required to fill the space without gaps or overlaps. They understand that a 1-unit by 1-unit by 1-unit cube is the standard unit for measuring volume. They select appropriate units, strategies, and tools for solving problems that involve estimating and measuring volume. They decompose three-dimensional shapes and find volumes of right rectangular prisms by viewing them as decomposed into layers of arrays of cubes. They measure necessary attributes of shapes in order to determine volumes to solve real world and mathematical problems.

#### **Grade 5 Overview**

#### Operations and Algebraic Thinking

- Write and interpret numerical expressions.
- Analyze patterns and relationships.

#### Number and Operations in Base Ten

- Understand the place value system.
- o Perform operations with multi-digit whole numbers and with decimals to hundredths.

#### Number and Operations—Fractions

- Use equivalent fractions as a strategy to add and subtract fractions.
- o Apply and extend previous understandings of multiplication and division to multiply and divide fractions.

#### Measurement and Data

- o Convert like measurement units within a given measurement system.
- o Represent and interpret data.
- Geometric measurement: understand concepts of volume and relate volume to multiplication and to addition.

#### Geometry

- o Graph points on the coordinate plane to solve real-world and mathematical problems.
- Classify two-dimensional figures into categories based on their properties.

# **Operations and Algebraic Thinking**

#### Write and interpret numerical expressions.

- 5.OA.1. Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.
- 5.OA.2. Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and 7, then multiply by 2" as 2 × (8 + 7). Recognize that 3 × (18932 + 921) is three times as large as 18932 + 921, without having to calculate the indicated sum or product.

#### Analyze patterns and relationships.

5.OA.3. Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane. For example, given the rule "Add 3" and the starting number 0, and given the rule "Add 6" and the starting number 0, generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so.

### **Number and Operations in Base Ten**

#### Understand the place value system.

- 5.NBT.1. Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.
- 5.NBT.2. Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.
- 5.NBT.3. Read, write, and compare decimals to thousandths.
  - Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g.,  $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$ .
  - Compare two decimals to thousandths based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.
- 5.NBT.4. Use place value understanding to round decimals to any place.

## Perform operations with multi-digit whole numbers and with decimals to hundredths.

- 5.NBT.5. Fluently multiply multi-digit whole numbers using the standard algorithm.
- 5.NBT.6. Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.
- 5.NBT.7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

# **Number and Operations—Fractions**

## Use equivalent fractions as a strategy to add and subtract fractions.

- 5.NOF.1. Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, 2/3 + 5/4 = 8/12 + 15/12 = 23/12. (In general, a/b + c/d = (ad + bc)/bd.)
- 5.NOF 2. Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers. For example, recognize an incorrect result 2/5 + 1/2 = 3/7, by observing that 3/7 < 1/2.

## Apply and extend previous understandings of multiplication and division to multiply and divide fractions.

- 5.NOF 3. Interpret a fraction as division of the numerator by the denominator ( $a/b = a \div b$ ). Solve word problems involving division of whole numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret 3/4 as the result of dividing 3 by 4, noting that 3/4 multiplied by 4 equals 3, and that when 3 wholes are shared equally among 4 people each person has a share of size 3/4. If 9 people want to share a 50-pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie?
- 5.NOF 4. Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction.
  - Interpret the product  $(a/b) \times q$  as a parts of a partition of q into b equal parts; equivalently, as the result of a sequence of operations  $a \times q \div b$ . For example, use a visual fraction model to show  $(2/3) \times 4 = 8/3$ , and create a story context for this equation. Do the same with  $(2/3) \times (4/5) = 8/15$ . (In general,  $(a/b) \times (c/d) = ac/bd$ .)

- Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.
- 5.NOF 5. Interpret multiplication as scaling (resizing), by:
  - Comparing the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication.
  - Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case); explaining why multiplying a given number by a fraction less than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence  $a/b = (n \times a)/(n \times b)$  to the effect of multiplying a/b by 1.
- 5.NOF 6. Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem.
- 5.NOF 7. Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions. [Students able to multiply fractions in general can develop strategies to divide fractions in general, by reasoning about the relationship between multiplication and division. But division of a fraction by a fraction is not a requirement at this grade.]
  - Interpret division of a unit fraction by a non-zero whole number, and compute such quotients. For example, create a story context for (1/3) ÷ 4, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that (1/3) ÷ 4 = 1/12 because (1/12) × 4 = 1/3.
  - Interpret division of a whole number by a unit fraction, and compute such quotients. For example, create a story context for  $4 \div (1/5)$ , and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that  $4 \div (1/5) = 20$  because  $20 \times (1/5) = 4$ .
  - Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem. For example, how much chocolate will each person get if 3 people share 1/2 lb of chocolate equally? How many 1/3-cup servings are in 2 cups of raisins?

# **Measurement and Data**

## Convert like measurement units within a given measurement system.

5.MD.1. Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.

#### Represent and interpret data.

5.MD.2. Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Use operations on fractions for this grade to solve problems involving information presented in line plots. For example, given different measurements of liquid in identical beakers, find the amount of liquid each beaker would contain if the total amount in all the beakers were redistributed equally.

## Geometric measurement: understand concepts of volume and relate volume to multiplication and to addition.

5.MD.3. Recognize volume as an attribute of solid figures and understand concepts of volume measurement.

- A cube with side length 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to measure volume.
- A solid figure which can be packed without gaps or overlaps using *n* unit cubes is said to have a volume of *n* cubic units.

5.MD.4. Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and improvised units.

5.MD.5. Relate volume to the operations of multiplication and addition and solve real world and mathematical problems involving volume.

- Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplying the height by the area of the base. Represent threefold whole-number products as volumes, e.g., to represent the associative property of multiplication.
- Apply the formulas  $V = I \times w \times h$  and  $V = b \times h$  for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real world and mathematical problems.
- Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real world problems.

# Geometry

#### Graph points on the coordinate plane to solve real-world and mathematical problems.

5.G,1. Use a pair of perpendicular number lines, called axes, to define a coordinate system, with the intersection of the lines (the origin) arranged to coincide with the 0 on each line and a given point in the plane located by using an ordered pair of numbers, called its coordinates. Understand that the first number indicates how far to travel from the origin in the direction of one axis, and the second number indicates how far to travel in the direction of the second axis, with the convention that the names of the two axes and the coordinates correspond (e.g., x-axis and x-coordinate, y-axis and y-coordinate).

5.G,2. Represent real world and mathematical problems by graphing points in the first quadrant of the coordinate plane, and interpret coordinate values of points in the context of the situation.

## Classify two-dimensional figures into categories based on their properties.

- 5.G,3. Understand that attributes belonging to a category of two-dimensional figures also belong to all subcategories of that category. For example, all rectangles have four right angles and squares are rectangles, so all squares have four right angles.
- 5.G,4. Classify two-dimensional figures in a hierarchy based on properties.



# **Implementation Guide – Grade 4 Mathematics**

Code: M.4.A.1 refers to: Mathematics -Grade 4 - Topic A - Skill 1

# CATEGORY: Operations and Algebraic Thinking. Standard: M.4.A.Use the four operations with whole numbers to solve problems

| Essential Questions                                                       | How will knowledge of problems solving help me function in everyday life?                             |  |
|---------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------|--|
| What should I be able to answer? What guides my thinking?                 | How do I choose which operation to use to solve a word problem?                                       |  |
|                                                                           | What strategies can I use to help me solve word problems?                                             |  |
| Assessment                                                                | Formative: Homework, board work, multiplication drill or bee,                                         |  |
| What will I be expected to know, understand, and be able to do in         | 3-2-1 summarizer/ 3-list strategies,2-give important things to look for when solving problem,1-       |  |
| order to demonstrate my learning?                                         | solution to the problem                                                                               |  |
|                                                                           |                                                                                                       |  |
|                                                                           | Summative – Chapter Test, quiz, performance assessment                                                |  |
| Skills                                                                    | M.4.A.1.Interpret a multiplication equation as a comparison, e.g. interpret 35 = 5 x 7 as a statement |  |
| What skills do I need to have in order to answer the essential questions? | that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of              |  |
|                                                                           | multiplicative comparisons as multiplication equations.                                               |  |
|                                                                           | M.4.A.2.Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using |  |

|                                                                                        | drawings and equations with a letter standing for the unknown quantity. Assess the                    |
|----------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------|
|                                                                                        | reasonableness of answers using mental computation and estimation strategies including rounding.      |
|                                                                                        | M.4.A.3. Solve multistep word problems posed with whole numbers and having whole-number               |
|                                                                                        | answers using the four operations, including problems in which remainders must be interpreted.        |
|                                                                                        | Represent these problems using equations with a letter standing for the unknown quantity. Assess      |
|                                                                                        | the reasonableness of answers using mental computation and estimation strategies including            |
|                                                                                        | rounding                                                                                              |
| Content                                                                                | Fluency in the multiplication facts 1 – 10, including visual and verbal representation e.g. If 3 boys |
| What content do I need to know in order to answer the essential                        | go to the store and buy 7 baseball cards and 7 boys go the store and buy 3 baseball cards. Did        |
| questions?                                                                             | they buy the same amount? Justify your answer.                                                        |
|                                                                                        | Missing factors e.g. 45 chairs were arranged in 5 rows. How many in each row? 5 x = 45                |
|                                                                                        | Strategies and Steps in Problem solving – draw a picture or model, make a table, diagram or list,     |
|                                                                                        | write an equation                                                                                     |
|                                                                                        | Inverse operations                                                                                    |
|                                                                                        | Estimation strategies – front end/clustering/rounding/rounding and adjusting/compatible numbers       |
| Integration of Learning How does this learning connect to my other areas (subjects) of | Economics – money                                                                                     |
|                                                                                        | Science – weights and measurements                                                                    |
| learning?                                                                              |                                                                                                       |
|                                                                                        |                                                                                                       |

| Tools for Learning                                         | KWL                                 |
|------------------------------------------------------------|-------------------------------------|
| Which tools will I use that will assist me in my learning? | Flash cards                         |
|                                                            | Dry Erase Board                     |
|                                                            | Games –Acting Out                   |
|                                                            | www.ixl.com/math/grade-4            |
|                                                            | The King's Chessboard – David Birch |

| Which 21st Century Skills are woven into this standa | rd?Critical Thinking/Problem Solving     | Collaboration         |
|------------------------------------------------------|------------------------------------------|-----------------------|
| •                                                    | Communications                           | Creativity/Innovatior |
| What level of rigor will I be using? (A, C)          | What level of relevance will I be using? | (B,D)                 |



# CATEGORY: Operations and Algebraic Thinking. Standard:M.4.B. Gain familiarity with factors and multiples.

| Essential Questions                                                                                            | What are the different ways I count?                                                             |  |
|----------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------|--|
| What should I be able to answer? What guides my thinking?                                                      | Why is it important for me to skip count?                                                        |  |
|                                                                                                                | What are prime and composite numbers?                                                            |  |
|                                                                                                                | How are factors and multiples related?                                                           |  |
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Formative – Board work                                                                           |  |
|                                                                                                                | Making a factor rainbow for 12 – connecting 1 and 12, 2 and 6, 3and 4                            |  |
|                                                                                                                | Quick write : list different factor pairs                                                        |  |
|                                                                                                                | Mad Minute drill                                                                                 |  |
|                                                                                                                | Summative – Chapter Test, quiz, performance assessment                                           |  |
| Skills                                                                                                         | M.4.B.1 Find all factor pairs for a whole number in the range 1-100. Recognize that a whole      |  |
| What skills do I need to have in order to answer the essential questions?                                      | number is a multiple of each of its factors. Determine whether a given whole number in the range |  |
|                                                                                                                | 1-100 is a multiple of a given one-digit number. Determine whether a given whole number in the   |  |
|                                                                                                                | range 1-100 is prime or composite.                                                               |  |

| Content What content do I need to know in order to answer the essential questions?               | Multiplication facts                                                                            |
|--------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------|
|                                                                                                  | Vocabulary: prime, composite, factor x factor = product, product ÷ factor = factor, multiple    |
|                                                                                                  | Multiple vs. Product                                                                            |
|                                                                                                  | Sieve of Eratosthenes                                                                           |
|                                                                                                  | Odds, evens and squares                                                                         |
|                                                                                                  | Area – build rectangles (arrays) with a given area can be 2 ways ex. 6 = 1x6 or x3x2: prime     |
|                                                                                                  | numbers have only 1 rectangle                                                                   |
|                                                                                                  | Ex. An ice cream truck visits a neighborhood every 4 days. She missed the truck today. When can |
|                                                                                                  | she expect it again.                                                                            |
| Integration of Learning How does this learning connect to my other areas (subjects) of learning? | Calendar – every 3 <sup>rd</sup> day you cut the lawn                                           |
|                                                                                                  | Science - measurement                                                                           |
|                                                                                                  |                                                                                                 |
| Tools for Learning Which tools will I use that will assist me in my learning?                    | Multiplication Table                                                                            |
|                                                                                                  | 100 Chart                                                                                       |
|                                                                                                  |                                                                                                 |

| Which 21 <sup>st</sup> Century Skills are woven into this standa | rd?Critical Thinking/Problem Solving     | c     | Collaboration         |
|------------------------------------------------------------------|------------------------------------------|-------|-----------------------|
| •                                                                | Communications                           |       | Creativity/Innovation |
| What level of rigor will I be using? (A, C)                      | What level of relevance will I be using? | (B.D) |                       |

# CATEGORY: Operations and Algebraic Thinking Standard: M.4.C. Generate and analyze patterns

| Essential Questions                                                       | Can I describe change mathematically?                                                                |  |
|---------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------|--|
| What should I be able to answer? What guides my thinking?                 | Can I describe numbers or objects that repeat mathematically?                                        |  |
|                                                                           |                                                                                                      |  |
| Assessment                                                                | Formative : Explore pattern problems                                                                 |  |
| What will I be expected to know, understand, and be able to do in         | Chapter test, quiz,Performance Assessment:                                                           |  |
| order to demonstrate my learning?                                         | Summative: Every Beat of Your Heart- The heart of a child below the age of twelve beats about        |  |
|                                                                           | 100 times a minute. Have the children find their pulse at rest for 1 minute. Then have them do       |  |
|                                                                           | some form of exercise, find their pulse for 1 minute. Then, have them run in place for 1 minute. Ask |  |
|                                                                           | follow up questions that predict what could happen for longer time or different activities.          |  |
| Skills                                                                    | M.4.C.1 Generate a number or shape pattern that follows a given rule. Identify apparent features of  |  |
| What skills do I need to have in order to answer the essential questions? | the pattern that were no explicit in the rule itself.                                                |  |
|                                                                           | For example, given the rule "Add 3" and the starting number 1, generate terms in the resulting       |  |
|                                                                           | sequence and observe that the terms appear to alternate between odd and even numbers. Explain        |  |
|                                                                           | informally why the numbers why the numbers will continue to alternate in this way.                   |  |

| Content What content do I need to know in                                               | Vocabulary: skip counting, multiple counting, sequences ex. Rule start with 2 and multiple by 3                                              |  |
|-----------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------|--|
| What content do I need to know in order to answer the essential                         | Model situations that the 4 operations of whole numbers as patterns. An operation can be "undone"                                            |  |
| questions?                                                                              | by its inverse.                                                                                                                              |  |
|                                                                                         | Represent a variable as an unknown quantity using a letter or symbol.                                                                        |  |
|                                                                                         | Develop an understanding of the Commutative and Associative Property ex. $3 \times 2 = 2 \times 3$                                           |  |
|                                                                                         | IN/OUT Tables                                                                                                                                |  |
| Integration of Learning                                                                 | Growth in tables and graphs using real world events                                                                                          |  |
| How does this learning connect to my other areas (subjects) of                          | How change is related to time (time tables)                                                                                                  |  |
| learning?                                                                               | Observing geometric patterns                                                                                                                 |  |
|                                                                                         | Patterns in science                                                                                                                          |  |
| Tools for Learning                                                                      | Pattern Blocks, or Tiles                                                                                                                     |  |
| Which tools will I use that will assist me in my learning?                              | Hundreds chart                                                                                                                               |  |
|                                                                                         | Calendar                                                                                                                                     |  |
|                                                                                         | Number line                                                                                                                                  |  |
|                                                                                         | The Patchwork Quilt – Valorie Flournoy                                                                                                       |  |
|                                                                                         | Performance assessment example:                                                                                                              |  |
|                                                                                         | www.rda.aps.edu/mathtaskbank/starthtm. Skip the Movie or Betty's Miniature Birdhouses                                                        |  |
| Which 21 <sup>st</sup> Century Skills are woven What level of rigor will I be using? (a | into this standard?Critical Thinking/Problem SolvingCollaborationCreativity/Innovation  A, C) What level of relevance will I be using? (B,D) |  |

# CATEGORY:Number and Operations in Base Ten. Standard: M.4.D. Generalize place value understanding for multi-digit whole numbers.

| Essential Questions                                                              | Can I express order and compare numbers?                                                                 |  |
|----------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------|--|
| What should I be able to answer? What guides my thinking?                        | Do I know the position of a digit in a number affects its value?                                         |  |
|                                                                                  |                                                                                                          |  |
| Assessment What will I be expected to know, understand, and be able to do in     | Formative – Board work, exit cards with solved problems, homework                                        |  |
| order to demonstrate my learning?                                                | Summative – Chapter test,quiz, performance assessment                                                    |  |
| Skills What skills do I need to have in order to answer the essential questions? | M.4.D.1. Recognize that in a multi-digit whole number, a digit in one place represents ten times         |  |
|                                                                                  | what it represents in the place to its right. For example, recognize that $700 \div 70 = 10$ by applying |  |
|                                                                                  | concepts of place value and division.                                                                    |  |
|                                                                                  | M.4.D.2. Read and write multi-digit whole numbers using base-ten numerals, number names, and             |  |
|                                                                                  | expanded form. Compare two multi-digit numbers based on meanings of the digits in each place,            |  |
|                                                                                  | using >, =, < symbols to record the results of comparisons.                                              |  |
|                                                                                  | M.4.D.3. Use place value understanding to round multi-digit whole numbers to any place.                  |  |

| Content What content do I need to know in order to answer the essential | Vocabulary: Place value names, period names, expanded form, rounding |
|-------------------------------------------------------------------------|----------------------------------------------------------------------|
|                                                                         | Discover patterns in place value                                     |
| questions?                                                              | Compare numbers using place value                                    |
|                                                                         | Using rounding to the nearest dollar to estimate costs               |
|                                                                         | Inverse operations                                                   |
| Integration of Learning                                                 | Social Studies -Population and Area                                  |
| How does this learning connect to my other areas (subjects) of          | Almanac Data - e.g. Tallest Buildings                                |
| learning?                                                               | Other number systems – Roman numerals, Chinese abacus                |
|                                                                         | Newspaper or magazine scavenger hunt for large numbers               |
|                                                                         | Consumer topics - estimating money                                   |
| Tools for Learning                                                      | Place Value Chart                                                    |
| Which tools will I use that will assist me in my learning?              | Number Line                                                          |
|                                                                         | Base Ten Blocks                                                      |
|                                                                         | Calculator                                                           |
|                                                                         | Napier Bones                                                         |
|                                                                         | Literature – How Much is Million – David Schwartz                    |
|                                                                         | Anno's Counting Book – Mitsumasa Anno                                |

| Which 21 <sup>st</sup> Century Skills are woven into this standar | rd?Critical Thinking/Problem Solving     | Collaboration         |
|-------------------------------------------------------------------|------------------------------------------|-----------------------|
|                                                                   | Communications                           | Creativity/Innovation |
| What level of rigor will I be using? (A, C)                       | What level of relevance will I be using? | _ (B,D)               |

CATEGORY: Number and Operations in Base Ten Standard: M.4.E. Use place value understanding and properties of operations to perform multi-digit arithmetic.

| Essential Questions What should I be able to answer? What guides my thinking?                                  | Do I know efficient methods for finding sums, differences, products and quotients?  Do I know what makes a strategy both effective and efficient?  Are my answers reasonable?                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |
|----------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Formative – board work, exit cards with problems, math journal writing, homework  Summative – chapter test, quiz, performance assessments                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |
| Skills What skills do I need to have in order to answer the essential questions?                               | M.4.E.1. Fluently add and subtract multi-digit whole numbers using the standard algorithm.  M.4.E.2. Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.  M.4.E.3. Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays and/or area models. |

| Content                                                                       | Properties –commutative, associative and distributive                                              |
|-------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------|
| What content do I need to know in order to answer the essential questions?    | Model multiplication using patterns (multiples of 10, 100 and 1,000), graph paper                  |
|                                                                               | Model division with base ten blocks and/or graph paper                                             |
|                                                                               | Vocabulary: factors, product, partial products, divisor, dividend, quotient, remainder, compatible |
|                                                                               | numbers                                                                                            |
|                                                                               | Using estimation to check reasonable answers                                                       |
|                                                                               | Break apart strategy ex. 3,456 3,000 + 400 + 50 + 6                                                |
|                                                                               | + 1,357 1,000 + 300 + 50 + 7                                                                       |
|                                                                               | $260 \div 4 = 200 \div 4 + 60 \div 4$                                                              |
| Integration of Learning                                                       | Consumer topics – money, shopping using advertisements, catalogue order forms, seating             |
| How does this learning connect to my other areas (subjects) of                | arrangements, compare shopping prices                                                              |
| learning?                                                                     | Averages (mean)                                                                                    |
|                                                                               | Lattice multiplication as enrichment                                                               |
| Tools for Learning Which tools will I use that will assist me in my learning? | Calculators – show how multiplication is repeated addition and division is repeated subtraction    |
|                                                                               | Base ten blocks used as area models                                                                |
|                                                                               | Literature – Anno's Mysterious Multiplying Jar – Anno                                              |
|                                                                               | A Remainder of One – Pinczes                                                                       |
|                                                                               |                                                                                                    |

# CATEGORY: Number and Operations - Fractions Standard: M.4.F. Extend understanding of fraction equivalence and ordering.

| Essential Questions                                               | Do I know when fractions and whole numbers used together in real life?                                                       |
|-------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------|
| What should I be able to answer? What guides my thinking?         | Can I model, compare and order fractions?                                                                                    |
| What galdes my tillhang.                                          | Do I know how are fractions alike and different?                                                                             |
| Assessment                                                        | Formative –Quick Write/Quick Draw – on the right draw a picture of the fraction and on the right explain                     |
| What will I be expected to know, understand, and be able to do in | what it means.                                                                                                               |
| order to demonstrate my learning?                                 | Model - !/2 is the same as 2/4,3/6 and 4/8 in arrays and on the number line                                                  |
|                                                                   | Students fold paper rectangles into thirds, shading 2/3 of the rectangles. Students refold the papers into                   |
|                                                                   | thirds and then in halves opening the rectangles to see that 4/6 are now shaded. Students look at the                        |
|                                                                   | displayed fractionsas 2/3, (2x2)(2x3), and 4/6 and reason that when the denominator and numerator are                        |
|                                                                   | multiplied by the same number the resulting fraction is equivalent to the original as shown by the shaded                    |
|                                                                   | rectangles. Summative - Chapter test, quiz, performance assessment                                                           |
| Skills                                                            | M.4.F.1. Explain why fraction $a/b$ is equivalent to a fraction $(n \times a)/(n \times b)$ by using visual fraction models, |
| What skills do I need to have in order to answer the essential    | with attention to how the number and size of the parts differ even though the two fractions themselves are                   |
| questions?                                                        | the same size. Use this principle to recognize and generate equivalent fractions.                                            |
|                                                                   | M.4.F.2. Compare two fractions with different numerators and different denominators, e.g., by creating                       |
|                                                                   | common denominators or numerators, or by comparing to a benchmark fraction such as ½. Recognize that                         |
|                                                                   | comparisons are valid only when the two fractions refer to the same whole. Record the results of                             |
|                                                                   | comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction                           |
|                                                                   | model.                                                                                                                       |

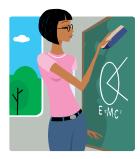
| Content                                                                  | Fractions are limited with denominators of 2,3,4,5,6,8,10,12, and 100.                                                     |  |
|--------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------|--|
| What content do I need to know in order to answer the essential          |                                                                                                                            |  |
|                                                                          | Compare fractions with <b>like</b> denominators by comparing the numerators.                                               |  |
| questions?                                                               | Compare fractions with <b>different</b> denominators by multiplying the numerator and denominator by 1                     |  |
|                                                                          | renaming as 2/2,3/3 etc.                                                                                                   |  |
|                                                                          | Example: Is 5/6 > 1/2 ? 3/6 = ½ than 5/6 > 3/6 therefore 5/6 > 1/2                                                         |  |
|                                                                          | Visual pictures of 2 fractions that make a whole. e.g. $\frac{1}{2} + \frac{1}{2} = 1$ and $\frac{1}{4} + \frac{3}{4} = 1$ |  |
|                                                                          | Example: If each person at a party will eat 3/8 of a pound of turkey and there are 5 people at the                         |  |
|                                                                          | party, how many pounds of turkey will be needed? Between what 2 whole numbers does your                                    |  |
|                                                                          | answer lie?                                                                                                                |  |
| Integration of Learning                                                  | Recipes                                                                                                                    |  |
| How does this learning connect to my other areas (subjects) of learning? | Carpentry                                                                                                                  |  |
| Tools for Learning                                                       | Fraction bars to compare Number lines, ruler                                                                               |  |
| Which tools will I use that will assist me in my learning?               | Pattern blocks Legos                                                                                                       |  |
|                                                                          | Quilts visual fractions. com                                                                                               |  |
|                                                                          | Literature – Fraction Action by Leedy                                                                                      |  |
|                                                                          | Fraction Fun by Adler                                                                                                      |  |
| Which 21 <sup>st</sup> Century Skills are wover                          | into this standard?Critical Thinking/Problem SolvingCollaboration Communications Creativity/Innovation                     |  |
| What level of rigor will I be using? (                                   | A, C) What level of relevance will I be using? (B,D)                                                                       |  |

CATEGORY: Number and Operations - Fractions Standard: M.4.G. Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.

| Essential Questions What should I be able to answer? What guides my thinking?                                  | Do I know how fractions are represented in everyday life?  Do I know if the computation with fractions and whole numbers the same or different?                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |  |
|----------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Exit cards                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |  |
| Skills What skills do I need to have in order to answer the essential questions?                               | <ul> <li>Summative – Chapter tests, quiz performance assessment</li> <li>M.4.G.1. Understand a fraction a/b with a &gt; 1 as a sum of fractions 1/b.</li> <li>a. Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.</li> <li>b. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. Examples: 3/8 = 1/8 + 1/8 + 1/8; 3/8 = 1/8 + 2/8; 2 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8.</li> <li>c. Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction.</li> <li>d. Solve word problems involving addition and subtraction of fractions referring to the same whole</li> </ul> |  |

|                                                                 | and having like denominators, e.g., by using visual fraction models and equations to represent the                  |
|-----------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------|
|                                                                 |                                                                                                                     |
|                                                                 | problem.                                                                                                            |
|                                                                 |                                                                                                                     |
|                                                                 | M.4.G.2. Apply and extend previous understanding of multiplication to multiply a fraction by a whole                |
|                                                                 | number.                                                                                                             |
|                                                                 | a. Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to                      |
|                                                                 | represent 5/4 as the product 5 x $\frac{1}{4}$ , recording the conclusion by the equation 5/4 = 5 x $\frac{1}{4}$ . |
|                                                                 | b. Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a                      |
|                                                                 | fraction by a whole number. For example, use a visual fraction model to express 3 x (2/5) as 6 x                    |
|                                                                 | (1/5), recognizing this product as 6/5. (In general, $n \times (a/b) = (n \times a)/b$ .)                           |
|                                                                 | c. Solve word problems involving multiplication of a fraction by a whole number, e.g., by using                     |
|                                                                 | visual fraction models and equations to represent the problem. For example, if each person at a                     |
|                                                                 | party will eat 3/8 of a pound of roast beef, and there will be 5 people at the party, how many                      |
|                                                                 | pounds of roast beef will be needed? Between what two whole numbers does your answer lie?                           |
| Content                                                         | Unit fractions                                                                                                      |
| What content do I need to know in order to answer the essential | Add and subtract fractional numbers with like denominators, using equivalent fractions. Example: 1                  |
| questions?                                                      | 1/4 - 3/4                                                                                                           |
|                                                                 | If $4/4 + \frac{1}{4} = \frac{5}{4}$ than $\frac{5}{4} - \frac{3}{4} = \frac{2}{4} = \frac{1}{2}$                   |
|                                                                 | Find fractional part of a given set or area. Model this example: $3 \times 2/5$ is the same as $6 \times 1/5 = 6/5$ |

| Integration of Learning                                        | Recipes                                                                                                  |
|----------------------------------------------------------------|----------------------------------------------------------------------------------------------------------|
| How does this learning connect to my other areas (subjects) of | Carpentry                                                                                                |
| learning?                                                      | Money                                                                                                    |
|                                                                | Probability                                                                                              |
|                                                                |                                                                                                          |
| Tools for Learning                                             | Graph paper, place value charts with decimals, number line                                               |
| Which tools will I use that will assist me in my learning?     | Fractions in Action Teacher Web Home Page                                                                |
|                                                                |                                                                                                          |
| Which 21 <sup>st</sup> Century Skills are woven                | n into this standard?Critical Thinking/Problem SolvingCollaboration Communications Creativity/Innovation |
| What level of rigor will I be using? (                         | <del></del>                                                                                              |



CATEGORY: Number and Operations - Fractions Standard: M.4.H. Understand decimal notation for fractions, and compare decimal fractions.

| Essential Questions What should I be able to answer? What guides my thinking?                                  | How can I numbers be expressed in multiple ways? How are fractions and decimals related?                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
|----------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Formative – Whiteboard work showing fractions above a number line and decimal equivalent below the line.  "I have, Who has"  Summative – Chapter test, quiz, performance assessment                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |
| Skills What skills do I need to have in order to answer the essential questions?                               | M.4.H.1. Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. [Students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators in general. But addition and subtraction with unlike denominators in general is not a requirement at this grade.] For example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100. M.4.H.2. Use decimal notation for fractions with denominators 10 or 100. For examples, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram. M.4.H.3 Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual model. |

| Content What content do I need to know in order to answer the essential questions?               | Compare fractions and decimals using models of hundred squares and base ten blocks Identify and understand the relationship between fractions and decimals Use number line to connect fractions and decimals. Use base ten blocks to connect 3/10 or 3 longs is the same as 30/100 |
|--------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Integration of Learning How does this learning connect to my other areas (subjects) of learning? | Money Batting averages Use the computer to draw circle graphs – and the web site create a graph                                                                                                                                                                                    |
| Tools for Learning Which tools will I use that will assist me in my learning?                    | Physical models, pictures, number lines, use both customary and centimeter rulers, coins  Base ten blocks  Graph paper  Nlvm.usu.edu                                                                                                                                               |

| Which 21 <sup>st</sup> Century Skills are woven into this standar | rd?Critical Thinking/Problem Solving     | Collaboration         |
|-------------------------------------------------------------------|------------------------------------------|-----------------------|
|                                                                   | Communications                           | Creativity/Innovation |
| What level of rigor will I be using? (A, C)                       | What level of relevance will I be using? | _ (B,D)               |

# CATEGORY: Measurement and Data. Standard: M.4.I. Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.

| Essential Questions                                               | How do I use measurements on a daily basis?                                                         |
|-------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------|
| What should I be able to answer? What guides my thinking?         | Are there different systems for measuring things?                                                   |
|                                                                   | Can I relate smaller units of measurement to larger ones?                                           |
|                                                                   |                                                                                                     |
|                                                                   |                                                                                                     |
| Assessment                                                        | Formative: Use a dry erase board to have the students display answers to equivalent                 |
| What will I be expected to know, understand, and be able to do in | measurements. Example: How many inches = 1 foot? Can 3 feet be equivalent to another unit of        |
| order to demonstrate my learning?                                 | measurement? Have students model units of measurement.                                              |
|                                                                   | Summative: Have students design a real life situation problem using finding the perimeter or area   |
|                                                                   | of a rectangle. For example: fencing a yard, buying the correct amount of carpet for a room. Design |
|                                                                   | a blueprint for the first floor of a house. For instance, door size, window size, and room size.    |
| Skills                                                            | M.4.I. 1. Know relative sizes of measurement units within one system of units including km, m, cm;  |
| What skills do I need to have in order to answer the essential    | kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements    |
| questions?                                                        | in a larger unit in terms of a smaller unit. Record measurement equivalents in a two-column table.  |
|                                                                   | For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48   |
|                                                                   | in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3,  |
|                                                                   | 36),                                                                                                |
|                                                                   | M.4.I. 2. Use the four operations to solve word problems involving distances, intervals of time,    |
|                                                                   | liquid volumes, masses of objects, and money, including problems involving simple fractions or      |
|                                                                   | decimals, and problems that require expressing measurements given in a larger unit in terms of a    |

|                                                                          | that feature a measurement scale. <b>M.4.I.</b> 3. Apply the area and perimeter formulas for rectangles in real world and mathematical |
|--------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------|
|                                                                          |                                                                                                                                        |
|                                                                          | problems. For example, find the width of a rectangular room given the area of the flooring and the                                     |
|                                                                          | length, by viewing the area formula as a multiplication equation with an unknown factor.                                               |
| Content                                                                  | Knowledge of customary and metric systems for length, time, volume, and mass.                                                          |
| What content do I need to know in order to answer the essential          | Relationship between smaller and larger units of measure. Example: 1 ft is 12 times as long as 1                                       |
| questions?                                                               | in.                                                                                                                                    |
|                                                                          | How to apply the formula for area and perimeter of rectangles in real life situations. Example:                                        |
|                                                                          | Determining the amount of flooring for a room, or fencing for a yard.                                                                  |
|                                                                          | Make a conversion table for comparing related smaller and larger units.                                                                |
|                                                                          | Vocabulary: metric, convert, conversion table, perimeter, area, mass, volume.                                                          |
| Integration of Learning                                                  | Science- measuring and finding the mass of objects. Comparing measurements such as 16 ounces                                           |
| How does this learning connect to my other areas (subjects) of learning? | = 1 lb. 48 ounces = 3 lb. (3x16). Analyzing and interpreting data from experiments.                                                    |
| Tools for Learning                                                       | Conversion tables, metric stick, yardstick, websites, assorted books, manipulative, Scholastic                                         |
| Which tools will I use that will assist me in my learning?               | printable resources. Teacher created.com, AIMS                                                                                         |

# CATEGORY: Measurement and Data. Standard: M.4.J. Represent and interpret data.

| Essential Questions                                                                                            | What Is a line plot?                                                                            |
|----------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------|
| What should I be able to answer? What guides my thinking?                                                      | How can I use a line plot diagram to show data?                                                 |
|                                                                                                                | Do I know how to add and subtract fractions?                                                    |
|                                                                                                                | What does a fraction represent?                                                                 |
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Formative: Use a dry erase board to display a set of measurements in fractions of a unit. For   |
|                                                                                                                | example: ½, ¼, 1/8.                                                                             |
|                                                                                                                | Solve problems involving adding and subtraction fraction by using information presented in line |
|                                                                                                                | plots.                                                                                          |
|                                                                                                                | Summative: Project: Design a line plot to solve a word problem. For example: Find and interpret |
|                                                                                                                | the difference in length between the longest and shortest specimens in an insect collection.    |
| Skills What skills do I need to have in order to answer the essential questions?                               | Understanding of line plots                                                                     |
|                                                                                                                | Fractions, operations on fractions.                                                             |
|                                                                                                                |                                                                                                 |

| Content What content do I need to know in order to answer the essential questions?               | Vocabulary: line plot, fraction, data set                                                                                                                                                      |  |  |
|--------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|--|
| Integration of Learning How does this learning connect to my other areas (subjects) of learning? | Science-interpreting data and representing it by a line plot. Social Studies- Representing with a line plot how many years lapsed between two historical events located on the same time line? |  |  |
| Tools for Learning Which tools will I use that will assist me in my learning?                    | Websites, AIMS                                                                                                                                                                                 |  |  |
| Which 21 <sup>st</sup> Century Skills are woven What level of rigor will I be using? (           | CommunicationsCreativity/Innovation                                                                                                                                                            |  |  |

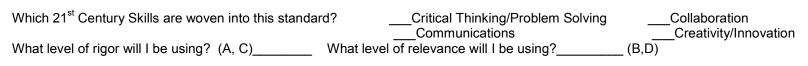
CATEGORY: Measurement and Data. Standard: M.4. K. Geometric measurement: Understanding concepts of angle and measure angles.

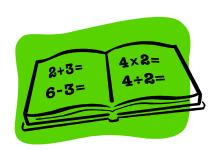
| Essential Questions                                                                                            | What geometric shapes do I know?                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |
|----------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| What should I be able to answer? What guides my thinking?                                                      | Where do I see geometric shapes everyday?                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
|                                                                                                                | What is an angle? How do I form an angle? Can I see angles in my daily life?                                                                                                                                                                                                                                                                                                                                                                                                                                                              |
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Formative: Be able to identify different types of angles; acute, obtuse, and right angles.  Students should be able to draw and measure various kinds of angles and geometric figures.  Summative: Project: Identify and label geometric shapes found in a real world and every day situation. For example: the classroom, street scene, the beach. The lifeguard stand has angles in the rungs, a one way street sign could be a ray, a stop sign could be an octagon, the hands on a clock could show an acute, obtuse, or right angle. |



| Skills What skills do I need to have in order to answer the essential questions? | M.4.K.1. Recognize angles as geometric shapes that are formed wherever two rays share a               |  |  |
|----------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------|--|--|
|                                                                                  | common endpoint, and understand concepts of angle measurement:                                        |  |  |
|                                                                                  | a. An angle is measured with reference to a circle with its center at the common endpoint of the      |  |  |
|                                                                                  | rays, by considering the fraction of the circular arc between the points where the two rays           |  |  |
|                                                                                  | intersect the circle. An angle that turns through 1/360 of a circle is called a "one-degree angle,"   |  |  |
|                                                                                  | and can be used to measure angles.                                                                    |  |  |
|                                                                                  | b. An angle that turns through $n$ one-degree angles is said to have an angle measure of $n$ degrees. |  |  |
|                                                                                  | M.4.K.2. Measure angles in whole-number degrees using a protractor. Sketch angles of specified        |  |  |
|                                                                                  | measure.                                                                                              |  |  |
|                                                                                  | M.4.K.3. Recognize angle measure as additive. When an angle is decomposed into non-overlapping        |  |  |
|                                                                                  | parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition   |  |  |
|                                                                                  | and subtraction problems to find unknown angles on a diagram in real world and mathematical           |  |  |
|                                                                                  | problems, e.g., by using an equation with a symbol for the unknown angle measure                      |  |  |
| Content                                                                          | Vocabulary: angle, acute angle, obtuse angle, right angle, rays, protractor.                          |  |  |
| What content do I need to know in order to answer the essential questions?       | Knowledge of relationship between an angle being 1/360 of a circle.                                   |  |  |
|                                                                                  | Knowledge of variables and how to substituting them in solving addition and subtraction problems to   |  |  |
|                                                                                  | find an unknown angle.                                                                                |  |  |
|                                                                                  |                                                                                                       |  |  |
|                                                                                  |                                                                                                       |  |  |
|                                                                                  |                                                                                                       |  |  |

| Integration of Learning How does this learning connect to my other areas (subjects) of learning? | Science-interpreting data using circle graphs. Social Studies- circle graphs. |
|--------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------|
| Tools for Learning Which tools will I use that will assist me in my learning?                    | Protractors, manipulatives, websites, dry erase boards, AIMS programs         |





# CATEGORY: Geometry: Standard: M.4.L. Draw and identify lines and angles, and classify shapes by properties of their lines and angels.

|                                                                                                                | What are lines made of? How can I draw a line?                                                      |  |
|----------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------|--|
| What should I be able to answer? What guides my thinking?                                                      | Do I know of different types of lines?                                                              |  |
|                                                                                                                | Can I identify lines in my world?                                                                   |  |
|                                                                                                                | Do I know what a line of symmetry is?                                                               |  |
| Assessment What will I be expected to know, understand, and be able to do in order to demonstrate my learning? | Formative: Use a dry erase board to practice drawing lines points, line segments, angles (right,    |  |
|                                                                                                                | acute, obtuse), perpendicular and parallel lines. Students should be able to identify and represent |  |
|                                                                                                                | two-dimensional figures.                                                                            |  |
|                                                                                                                | Use models, concrete objects and manipulatives to represent symmetry and lines of symmetry.         |  |
|                                                                                                                | Use protractors to draw and measure right angles and triangles.                                     |  |
|                                                                                                                | Summative: Project- Identify lines in the world. Example: train tracks, intersections, and parallel |  |
|                                                                                                                | streets.                                                                                            |  |
| Skills What skills do I need to have in order to answer the essential questions?                               | M.4.L. 1. Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular |  |
|                                                                                                                | and parallel lines. Identify these in two-dimensional figures.                                      |  |
|                                                                                                                | M.4.L. 2. Classify two-dimensional figures based on the presence or absence of parallel or          |  |
|                                                                                                                | perpendicular lines, or the presence or absence of angles of a specified size. Recognize right      |  |
|                                                                                                                | triangles as a category, and identify right triangles.                                              |  |
|                                                                                                                | M.4.L. 3. Recognize a line of symmetry for a two-dimensional figure as a line across the figure     |  |
|                                                                                                                | such that the figure can be folded along the line into matching parts. Identify line-symmetric      |  |
|                                                                                                                | figures and draw lines of symmetry.                                                                 |  |
|                                                                                                                |                                                                                                     |  |

| Content What content do I need to know in order to answer the essential questions?               | Vocabulary: point, line, parallel lines, perpendicular lines, symmetry, lines of symmetry, triangle, right triangle, angels.                                                         |
|--------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Integration of Learning How does this learning connect to my other areas (subjects) of learning? | Science: constructing tables, charts to represent data. Social Studies: identifying borders, rivers, how the states fit with each other. Art: What's in a name? Perspective drawing. |
| <b>Tools for Learning</b> Which tools will I use that will assist me in my learning?             | Ruler, protractor, commercial websites.                                                                                                                                              |
|                                                                                                  |                                                                                                                                                                                      |

| Which 21 <sup>st</sup> Century Skills are woven into this standar | d?Critical Thinking/Problem Solving      | Co      | llaboration          |
|-------------------------------------------------------------------|------------------------------------------|---------|----------------------|
|                                                                   | Communications                           | Cı      | reativity/Innovation |
| What level of rigor will I be using? (A, C)                       | What level of relevance will I be using? | _ (B,D) |                      |



# Assessment and Grading

# **Grading and Assessment**

## **Report Cards**



- Report cards will not be grade specific.
  - o **Kindergarten** students will receive reports aligned to the skills appropriate to that level.
  - Students in **grades 1 3** will receive the primary form of the report card.
    - The grading system will continue as letter grades.
    - No numerical equivalents are attached to these grades.
  - The children in grades 4 8 will receive the elementary form of the report card
    - The grading system will continue as number grades for major content areas: Religion, Math and English Language Arts, Science and Social Studies. The general average is calculated from these grades.
    - A number scale is used for other content areas: Art, Music, Physical Education, Technology and World Language.

#### Grading Practices:

- o The students will receive **one grade** for ELA and **one grade** for Math
  - The overall grade for each of these content areas will be an average of the progress shown in all of the "subset" categories for that content area.
  - ELA -- Care must be taken to ensure that the assessments reflect the entirety of ELA
    - At a minimum 2 assessments must be planned to assess progress in each of the sub-categories.
    - In each "sub-category":
      - o a "+" will indicate that the student meets or exceeds expectations in that area.
      - o a " $\sqrt{}$ " will indicate that the student continues to work towards meeting expectations.
  - In **Math**, the students will again receive one overall grade.
    - Progress in sub-categories" will be noted with a "+" or a " $\sqrt{}$ " as indicated above.
    - Progress should be able to documented by at least two different assessments in each area.



#### **Portfolios:**

- o Portfolio assessment is a "perfect fit" with the Core Curriculum State Standards
- o Portfolios should be used to gather relevant samples of student work over time
- o Students are involved in the selection of artifacts
  - Students do self-reflection of their work
  - Teachers and students periodically discuss the work contained in the portfolio

#### Minimum Requirements for Student Portfolios:

- Baseline writing samples start and end of school year
- o 2 ELA Performance assessments (all stages with rubric attached.)
- 2 Math Performance assessments
- Standardized test scores
- Social Studies, Science, Art, Technology, Music, World Language samples
- o Student Choices with entry slip attached
- Other items deemed necessary by the local school
  - Writing pieces
  - Science experiments
  - Mathematics problems and solutions
  - Applied Mathematics
  - Book reviews
  - Research projects
  - Physical Fitness Summary
  - Interdisciplinary projects/assignments





#### Web site for Common Core Standards:

http://www.corestandards.org/the-standards/

 Resources aligned to the Common Core Standards can be found at: http://teacherweb.com/PA/AOP/ETCC/apt1.aspx

You will find a wealth of resources related to curriculum on the following Curriculum Committee web sites.

- Curriculum web site:
  - http://www.teacherweb.com/PA/AOP/ElementaryCurriculumandInstruction/h1.aspx English Language Arts web site:
  - http://www.teacherweb.com/PA/AOP/ElementaryIntegratedLanguageArts%28ILA%29/ap2.aspx
- Mathematics web site:
  - http://www.teacherweb.com/PA/AOP/ElementaryMathematicsCurriculumCommittee/apt1.aspx
- Library Media web site:
  - http://www.teacherweb.com/PA/AOP/ElementaryLibraryMediaCommittee/h0.stm
- Early Childhood web site: http://www.teacherweb.com/PA/AOP/EarlyChildhood/
- Assessment: <a href="http://www.teacherweb.com/PA/AOP/ElementaryAssessmentCommittee/ap1.aspx">http://www.teacherweb.com/PA/AOP/ElementaryAssessmentCommittee/ap1.aspx</a>